# The Macro Neutrality of Exchange-Rate Regimes in the presence of Exporter-Importer Firms

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#### Abstract

I characterize exchange-rate regime breaks for thirty countries between 1960 and 2019, and I establish that while they affect the volatilities of nominal and real exchange rates they do not change the volatilities of other real macro variables (output, consumption, investment, and net exports). This is true even in countries in which exports and imports represent a large component of gross domestic product. I document that current leading models of exchange rate determination cannot match these facts. I propose a model with financial frictions and exporter-importer firms which matches the behavior of nominal and real exchange rates and real macro variables across exchange-rate regimes, even for economies in which the sum of exports and imports exceeds gross domestic product.

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### **1** Introduction

A substantial body of literature in the field of international macroeconomics and finance seeks to assess the impact of exchange-rate regimes on real macro variables (Friedman 1953, Mussa 1986, Baxter and Stockman 1989). The central natural experiment under examination in this body of literature revolves around the upheaval in the US monetary regime following the collapse of the Bretton Woods system in 1973. Consequently, the bulk of research findings in this field trace their origins to an exogenous shock that transpired fifty years ago, and affected the United States whose modest volume of international trade in proportion to its overall economic output is an outlier.

My approach is to focus on natural experiments beyond the breakdown of the Bretton Woods system. Furthermore, I focus on countries with relatively higher volumes of international trade compared to the United States. This perspective contributes a novel dimension to our understanding of macro dynamics when exchange-rate regimes change. I propose a characterization of exchange-rate regimes based on the trade-weighted exchange rates of thirty countries from 1957 to 2019. For all these economies, I show that structural breaks in the volatility of nominal exchange rates are systematically associated with structural breaks in the volatility of real exchange rates.

I use this large panel of volatility breaks to document a muted reaction to exchange-rate regime breaks of several real macro variables (output, consumption, investment, and net exports), but not the real exchange rate. The reaction is muted even though I consider countries that have more exports and imports, compared to total output, than the United States. In the United States, the amount of international trade—that is, exports plus imports—is relatively small compared to total output, with an average trade-to-GDP ratio of about 16% between 1960 and 2019; in contrast, Belgium, one of the countries that I consider, has an average trade-to-GDP ratio of about 101% over the same period.

I show that leading models of exchange rate determination, and even those specifically designed to study exchangerate regime breaks, do not match the evidence that I put forward. I then propose a model that can match the facts based on financial frictions and the presence of exporter-importer firms. Financial frictions in the form of segmented markets break the Backus and Smith (1993) condition, allowing for a possible disconnect between the real exchange rate and macro variables. Yet, this is not sufficient since exports and imports would still be too volatile and connected to the real exchange rate. Aside from this being directly counterfactual to the data, it can only generate a low reaction of macro variables (like output) to real exchange rates for those economies that are calibrated to be relatively closed to the international trade. I show that for economies with higher trade-to-GDP ratios than the United States, output would inherit the excess volatility of exports and imports. Accounting for exporter-importer firms is key to match the observed muted reaction of macro variables to real–exchange rate movements. This is true in the aggregate for countries such as Belgium, but it is also true for countries such as the United States once I restrict the focus to exports and imports. I show that for the United States, the overall muted response results from a mix of a counterfactually large response of exporters and importers, with these firms being a small fraction of the overall economy. The general equilibrium model is able to reconnect the macro empirical regularities from the international finance literature to a theoretical mechanism that is grounded in the micro empirical evidence of international trade, establishing how this micro mechanism is pivotal for the explanation of the macro empirical regularities. This broaderlevel contribution complements a recent literature which emphasizes the importance of fluctuations coming from the real economy in the class of general equilibrium models with international financial-market segmentation. Specifically, Kekre and Lenel (2024) shows that, while shocks from segmented financial markets play a meaningful role at high frequencies, persistent shocks to relative demand from the real economy have a dominant role in driving the nominal exchange rate.

In the first part of the paper, Section 2.1, using trade-weighted exchange rates covering thirty countries from 1957 to 2019, I characterize exchange-rate regimes based on a statistical approach only. In bilateral exchange-rate classifications, the definition of exchange-rate regime for a given country relies only on its central bank's decision to keep the currency either floating or pegged to a reference currency. Therefore, bilateral exchange-rate classifications (e.g., Petracchi 2022) identify exchange-rate regime breaks only when one of the two central banks changes its decision and induces a simultaneous volatility break in the bilateral series of nominal and real exchange rates.

Instead, in Section 2.1, I identify the structural breaks in the volatility of the trade-weighted nominal and real exchange rates separately, using the structural break test developed by Lavielle (1999) and Lavielle and Moulines (2000). This results in a richer set of exchange-rate regime breaks which includes several countries—for example, Belgium which would have been excluded using bilateral exchange-rate classifications. The main finding is that every break in the set of structural breaks in the volatility of the nominal trade-weighted exchange-rate series corresponds to a structural break in the volatility of the real trade-weighted exchange-rate series.

In Section 2.2, I consider how real macro variables react to exchange-rate regime breaks when considering all thirty countries in my sample, which covers sixty-two exchange-rate regime breaks from 1957 to 2019. A robust finding is that the volatilities of all real macro variables show no statistically significant change across breaks, with a single exception: the real exchange rate. Crucially, this result does not depend the amount of exports and imports by countries. The challenge is to explain why, when a country moves from a pegged to a floating regime, the resulting volatility of the exchange rates is not transmitted to other real macro variables. We have to question if we are able to find a set of assumptions that ensure the consistency of a theoretical model with the empirical evidence for a country such as Belgium with an average trade-to-GDP ratio of about 101%.<sup>1</sup>

Therefore, finding such a set of assumptions would ensure the generality of the theoretical model in Section 3, for a large set of countries presenting a higher average trade-to-GDP ratios than the United States. I find that three assumptions are sufficient.

<sup>&</sup>lt;sup>1</sup>Belgium has a higher average trade-to-GDP ratio than the United States, but it is not an outlier. For instance, Czech Republic, Latvia, or Slovenia have even higher average trade-to-GDP ratios; see Panels (c) and (d) of Figure 2.

- International financial markets are imperfect, following Gabaix and Maggiori (2015). In any complete-market
  model, the condition of efficient risk sharing tends to make the consumption difference co-move with the real
  exchange rate. But this result is invalidated by several empirical studies (e.g., Backus and Smith 1993). This
  assumption also guarantees that the model matches a set of empirical facts from the finance literature, the
  most relevant of which is room for deviations from uncovered interest parity (see Fama 1984).
- 2. There are deviations from the law of one price in the form of variable markups and pricing to market, following the empirical industrial-organization literature.<sup>2</sup> Though this assumption helps to improve the fit of theoretical models to the muted reaction of real macro variables to real–exchange rate movements, it is not sufficient.

In the calibration section, using data on Belgium, Sweden, South Korea, and the United Kingdom, I show that only assuming imperfect international financial markets and deviations from the law of one price as in Itskhoki and Mukhin (2021) and Itskhoki and Mukhin (2025) is not enough to match the observed muted reaction. Additionally, I also show that modeling without exporter-importer firms misses an important feature of the US data: it is unable to capture the muted reaction of either exports or imports to exchange rate movements when they are treated separately. Under a floating regime, exchange rates are highly volatile and exporters are not able to prevent exports from responding to exchange rates, although they can adjust their markups and price also in terms of the local competitors.

3. Exporters are simultaneously importers (Bernard et al. 2007, Amiti, Itskhoki, and Konings 2014, Albornoz and Garcia-Lembergman 2020, Barbiero 2022, Blaum 2024, Wicht and Yeşin 2025). This feature, coming from the empirical evidence in international trade, is the key ingredient to match the observed muted reaction in an economy with a large amount of exports and imports, compared to total output, in a general equilibrium model. First, in Section 3.2, I prove with a theoretical proposition that this salient feature can completely disconnect real macro variables from nominal and real exchange rates in the limit. Second, in Section 3.3, using data on Belgium between 1960 and 2019 and a transparent calibration of the import intensity of the exporter-importer firms, I show that my model with exporter-importer firms can reproduce the co-movement of nominal and real exchange rates and the muted reaction of real macro variables. Additionally, I show that it is able to capture the muted reaction of either exports or imports to exchange rate movements, when they are treated separately, for the United States. Lastly, I document that such a feature of trade is not peculiar to a specific country, providing cross-country empirical evidence in support of exporter-importer firms in Section 3.4.

<sup>&</sup>lt;sup>2</sup>For instance, Goldberg and Verboven (2001, 2005) find not only that the law of one price does not hold, but also that firms absorb the exchange-rate fluctuations thanks to a local component of their marginal costs and markup adjustment.

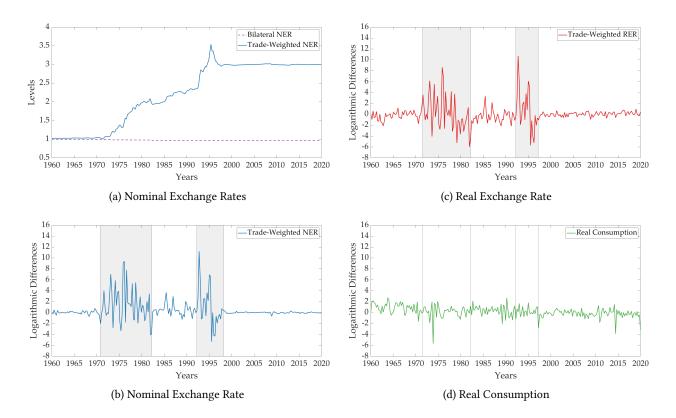


Figure 1: Exchange Rates and Real Consumption in Belgium (1960-2019)

*Notes for Panels (a) and (b):* The bilateral nominal–exchange rate series between Belgium and Germany is dashed and in magenta, and the trade-weighted nominal–exchange rate series between Belgium and the rest of the world is in blue; I normalize the two series such that they are both equal to 1 in the first quarter of 1960. The vertical lines represent exchange-rate regime breaks identified in the trade-weighted nominal–exchange rate series in logarithmic difference. I shade the periods with floating regimes in the trade-weighted nominal–exchange rate series. *Notes for Panels (c) and (d):* The trade-weighted real–exchange rate series is in red and the real consumption-difference series is in green. The

vertical lines represent exchange-rate regime breaks identified in the trade-weighted real-exchange rate series in logarithmic difference. I shade the periods with floating regimes in the trade-weighted real-exchange rate series.

Sources: The Bank of Italy's Exchange Rates Portal, the International Monetary Fund's Direction of Trade Statistics and International Financial Statistics, and the Organisation for Economic Co-operation and Development's OECD.Stat. For details, see Section 2.

Figure 1, depicting time series for Belgium between 1960 and 2019, motivates my work and illustrates the gains deriving from my characterization of exchange-rate regimes based on a statistical approach to trade-weighted exchange rates. Panel (a) plots the bilateral nominal exchange rate between Belgium and Germany, the reference country for the Belgian economy, (dashed) and the trade-weighted nominal exchange rate between Belgium and the rest of the world. Both series are in levels, at a quarterly frequency. Panel (b) plots the trade-weighted nominal exchange rate between Belgium and the rest of the world in logarithmic difference, at a quarterly frequency.

Belgium's regime is typically considered pegged for the entire period in standard bilateral classifications.<sup>3</sup> Indeed, it was pegged if one considers the bilateral nominal exchange rate between Belgium and Germany as shown in Panel (a). But if one considers the trade-weighted nominal exchange rate between Belgium and the rest of the world, the picture completely changes and this is the pivotal advantage of my characterization of exchange-rate regimes.

<sup>&</sup>lt;sup>3</sup>See Levy-Yeyati and Sturzenegger (2005), Klein and Shambaugh (2010), Ilzetzki, Reinhart, and Rogoff (2019), and Petracchi (2022).

In Panel (b), using the test developed by Lavielle (1999) and Lavielle and Moulines (2000), I identify four structural breaks in volatility that define five exchange-rate regimes: a pegged regime from 1960 to 1970, a floating regime from 1970 to 1982, a pegged regime from 1982 to 1992, a floating regime from 1992 to 1998, and a pegged regime from 1998 to 2019. Crucially, the four exchange-rate regime breaks are present not because of Belgian-German bilateral exchange-rate regime breaks but because of Belgium's trading partners, which experienced exchange-rate regime breaks in relation to Germany; as a consequence, they can be interpreted as shocks exogenous to Belgian monetary policy and economic conditions, offering a setting to identify the effects of different exchange-rate regimes.

Panels (c) and (d) in Figure 1 plot Belgium's trade-weighted real-exchange rate series and its real-consumptiondifference series respectively, at a quarterly frequency, between 1960 and 2019. Both series are in logarithmic difference and represent Belgium versus the rest of the world. The trade-weighted real-exchange rate series presents four structural breaks in volatility, corresponding to the four exchange-rate regime breaks in the Belgian trade-weighted nominal exchange rate. Meanwhile, the real-consumption-difference series presents no structural breaks; the shocks do not alter the volatility of the real-consumption-difference series, even in an economy with a large amount of exports and imports compared to total output.

**Related Literature.** My paper contributes to several strands of the literature. First, the characterization of exchange-rate regimes in the context of trade-weighted exchange rates goes beyond the monetary non-neutrality arising from bilateral exchange rates as seen in the Mussa puzzle (Mussa 1986) and its generalization (Petracchi 2022).<sup>4</sup> Second, my analysis of real macro variables in relation to exchange-rate regime breaks connects to a large literature on exchange rates and macro outcomes (Friedman 1953, Meese and Rogoff 1983, Fama 1984, Baxter and Stockman 1989, Cole and Obstfeld 1991, Backus and Smith 1993, Obstfeld and Rogoff 2000, Farhi and Gabaix 2015, Lustig and Verdelhan 2019, Amador et al. 2020, Itskhoki and Mukhin 2021, Engel and Wu 2022, Lilley, Maggiori, and Schreger 2022 ,and Kekre and Lenel 2024). My theoretical model is related to the exchange rate portfolio-balance literature (Kouri 1976, Jeanne and Rose 2002, Gabaix and Maggiori 2015, Cavallino 2019, Maggiori 2022, Bacchetta, Benhima, and Berthold 2023, Bacchetta, Davis, and van Wincoop 2023) and the literature that evaluates the effects of different exchange-rate regimes (Monacelli 2004, Benigno and Benigno 2008, Ayres, Hevia, and Nicolini 2021, Flaccadoro and Nispi Landi 2022, and Itskhoki and Mukhin 2025). It is also related to the international-trade literature using firm-product-level imports and export data (Bernard et al. 2007, Amiti, Itskhoki, and Konings 2014, Albornoz and Garcia-Lembergman 2020, Barbiero 2022, Blaum 2024, Wicht and Yeşin 2025).

<sup>&</sup>lt;sup>4</sup>Using bilateral time series primarily on the United States and thirteen advanced countries between 1957 and 1984, Mussa (1986) documents what is now referred to as the Mussa Puzzle: the 1973 breakdown of the Bretton Woods system increased the volatility of not only the nominal US-dollar exchange rate but the real US-dollar exchange rate, which implies monetary non-neutrality. Petracchi (2022), using data covering forty-four countries from 1954 to 2019, finds that the Mussa puzzle is generalizable: any break in an exchange-rate regime that changes the volatility of the bilateral nominal exchange rate also changes the volatility of the bilateral real exchange rate. More recently, compiling a novel dataset of product-level prices in sixteen European countries starting in 1972, Petracchi, Mello, and Kim (2025) establishes that exchange-rate breaks affect both the volatility of the bilateral nominal exchange rates and the volatility of the product-level real exchange rates, without impacting on the volatility of relative prices significantly.

## 2 Empirical Facts and Exchange-Rate Regimes

In Section 2.1, I introduce a characterization of exchange-rate regimes, based on thirty countries from 1957 to 2019, and provide evidence for the Mussa puzzle—the fact that nominal and real exchange rates co-move across exchange-rate regimes—in the context of trade-weighted exchange rates. In Section 2.2, I consider real-macro-variable time series (output, consumption, investment, and net exports) of the thirty countries to show that exchange rate disconnect—that is, the muted reaction of real macro variables to real exchange-rate movements—remains persistent across exchange-rate regimes.<sup>5</sup>

**Data.** I use quarterly data covering the 1957-2019 period for thirty countries—twenty-four European countries and six non-European G20 countries. The choice of the countries for my empirical analysis is exclusively based on the availability of the historical time series for the real macro variables—output, consumption, investment, and net exports. However, complete data for all the countries are not available and a list of time periods for each country is in Table 10 in Appendix A.2. The twenty-four European countries include the twenty-one European Union member countries along with Norway, Switzerland, and the United Kingdom, while the six non-European G20 countries are Australia, Brazil, Canada, Japan, South Africa, and the United States.<sup>6</sup>

#### 2.1 A Characterization of Exchange-Rate Regimes

I begin by constructing trade-weighted exchange rates with a twofold purpose. First, they allow me to empirically evaluate the magnitude of exchange-rate fluctuations, for any given country in relation to its trading partners, which have to be considered in general equilibrium models. Second, they allow me to introduce a characterization of exchange-rate regimes, where I identify breaks in volatility through a heteroskedasticity-based approach only.

Monthly time-series data on bilateral nominal exchange rates come from the Exchange Rates Portal of the Bank of Italy; I use the Deutsche Mark as the reference currency for the studied European countries and the US dollar for the non-European G20 countries. I obtain the bilateral nominal–exchange-rate time series for each European country by combining the dollar/Deutsche Mark time series and the dollar/euro time series after December 2001, at which time 1 euro was worth 1.95583 Deutsche Marks, with the various other dollar/foreign-currency time series.<sup>7</sup> I then combine them, using the trade weights from the Direction of Trade Statistics of the International Monetary Fund, to obtain trade-weighted nominal exchange rates.<sup>8</sup>

<sup>&</sup>lt;sup>5</sup>The phrase "exchange rate disconnect" generically refers to the absence of correlation between exchange rates and other macro variables; see Obstfeld and Rogoff (2000).

<sup>&</sup>lt;sup>6</sup>The twenty-four studied member countries of the European Union are Austria, Belgium, the Czech Republic, Denmark, Estonia, Finland, France, Germany (West Germany before October 1990), Greece, Ireland, Italy, Latvia, Lithuania, Luxembourg, the Netherlands, Poland, Portugal, the Slovak Republic, Slovenia, Spain, and Sweden.

 $<sup>^{7}</sup>$ If a currency was renominated—for example, the French franc in January 1960—I normalized the series in order to remove the ensuing jump.

<sup>&</sup>lt;sup>8</sup>For any given country, I use as weights the mean values of its exports and imports, averaged over the 1957-2019 period, to and from Australia, Austria, Belgium, Canada, Denmark, Finland, France, Germany, Greece, Ireland, Italy, Japan, Luxembourg, the Netherlands, Norway, Portugal, Spain, Sweden, Switzerland, the United Kingdom, and the United States.

Finally, I combine the latter rates with monthly consumer price indexes (CPIs) from the International Monetary Fund's International Financial Statistics, using the same weights as above, to obtain CPI-based trade-weighted real exchange rates.<sup>9</sup>

Next, I identify the exchange-rate regime breaks by applying the heteroskedasticity-break test, developed by Lavielle (1999) and Lavielle and Moulines (2000), to the first difference of the logarithm of the nominal exchange rate,  $\mathcal{E}_t$ , and the first difference of the logarithm of the real exchange rate,  $\mathcal{Q}_t$ , separately. The first differences are defined as follows:

$$\Delta q_t = \Delta e_t + \pi_t^* - \pi_t.$$

Here,  $\Delta q_t = ln(\mathcal{Q}_t) - ln(\mathcal{Q}_{t-1})$ ,  $\Delta e_t = ln(\mathcal{E}_t) - ln(\mathcal{E}_{t-1})$ , and  $\pi_t^* - \pi_t$  is the difference between the inflation rate in the foreign country and the inflation rate in the rest of the world (home country).<sup>10</sup>

The same methodology by Lavielle (1999) and Lavielle and Moulines (2000) has been already applied to identify breaks using bilateral series of nominal and real exchange rates (see, for example, Petracchi 2022). However, the application to trade-weighted exchange rates results in a richer set of exchange-rate regimes than the application to bilateral exchange rates. Indeed, applying such a methodology to trade-weighted exchange rates can characterize exchange-rate regimes for countries which would have been excluded in bilateral exchange-rate classifications— namely, Austria, Belgium, the Czech Republic, Denmark, Estonia, Germany (reference-currency country for European countries in bilateral classification), Ireland, Luxembourg, the Netherlands, Poland, the Slovak Republic, and the United States (reference-currency country for non-European countries in bilateral classification).<sup>11</sup>

The test yields the results for Belgium that are reported in the third column of Table 1. Table 1, together with Table 11 in Appendix A.2.1, which reports the results for all the other studied countries, represents the first main empirical result of this paper. The heteroskedasticity-break test separately identifies structural breaks in the trade-weighted nominal– and real–exchange-rate series that characterize two types of exchange-rate regime: periods of low exchange-rate volatility and periods of high exchange-rate volatility. Then, periods of low exchange-rate volatility are assigned to pegged regimes and periods of high exchange-rate volatility are assigned to floating regimes.

<sup>&</sup>lt;sup>9</sup>For brevity, from here on, I use the phrase "the rest of the world" (home country) to indicate Australia, Austria, Belgium, Canada, Denmark, Finland, France, Germany, Greece, Ireland, Italy, Japan, Luxembourg, the Netherlands, Norway, Portugal, Spain, Sweden, Switzerland, the United Kingdom, and the United States; the term "nominal exchange rate" to refer to the trade-weighted nominal exchange rate; and the term "real exchange rate" to refer to the CPI-based trade-weighted real exchange rate.

<sup>&</sup>lt;sup>10</sup>A complete description of the Lavielle (1999) and Lavielle and Moulines (2000) test can be found in Appendix A.2.1.

<sup>&</sup>lt;sup>11</sup>Importantly, other papers—for instance, Morales-Zumaquero and Sosvilla-Rivero (2010)—propose characterizations of exchange-rate regimes using a heteroskedasticity-break test and real effective exchange rates (REERs) from the International Financial Statistics of the International Monetary Fund or the Data Portal of the Bank for International Settlements. However, although overcoming the limitation deriving from bilateral exchange-rate classifications, the use of these REEs ultimately biases the exchange-rate regime characterization for European countries. The reason of this can be found in the construction of the REERs from the International Financial Statistics of the International Monetary Fund or the Data Portal of the Bank for International Settlements, as the euro-area countries are considered as a single area (corresponding to a single trade weight) with an unique nominal exchange rate (corresponding to a simple average of their nominal exchange-rates) for periods before the introduction of the euro in January 1999. This bias ultimately undermines the identification of the exchange-rate regime breaks by the heteroskedasticity-break test, resulting in an underestimation of the breaks. An example of the bias is, indeed, the fact that Morales-Zumaquero and Sosvilla-Rivero (2010, p.145) detects only one exchange-rate regime break (January/February 1974) for Belgium, whereas my classification poses four breaks for Belgium in Table 1.

Nominal Exchange Rate	Real Exchange Rate	Exchange-Rate Regime
January 1957 - June 1971	January 1957 - July 1971	Pegged Regime
July 1971 - September 1978 October 1978 - July 1992	August 1971 - January 1982 February 1982 - July 1992	Floating Regime Pegged Regime
August 1992 - March 1998	August 1992 - March 1997	Floating Regime
April 1998 - December 2019	April 1997 - December 2019	Pegged Regime

Table 1: Exchange-Rate Regimes for Belgium

This characterization of exchange-rate regimes confirms the Mussa puzzle for the reference-currency countries (Germany and the United States) and countries that formally switched their exchange-rate regime from pegged to floating or vice versa (for example, Brazil). Remarkably, it also shows the puzzle for economies that never formally switched in the studied period (for example, Belgium). For two reasons, the characterization turns out to be crucial for understanding how exchange-rate regimes affect the real economy.

First, in economies that did not switch as Belgium, the exchange-rate regime breaks are exogenous to their monetary-policy decisions and domestic economic conditions, offering a better setting than the breakdown of the Bretton Woods system in 1973—that is an endogenous switch in the US monetary policy—to identify the effects of different exchange-rate regimes. This a stronger identification strategy than in a standard regression-discontinuity design (see, for instance Itskhoki and Mukhin 2025), in which identification does not rely on the exogeneity of the exchange-rate regime breaks but only requires that potential confounders evolve continuously around the breaks.

The literature on the exchange rate disconnect has traditionally focuses on countries such as Japan, Korea, New Zealand, Sweden, the United Kingdom, and the United States, for which the mean import-to-GDP ratios are relatively low (e.g. below 35%).<sup>12</sup> In contrast, I identify exchange-rate regime breaks for countries for which exports and imports are relatively large compared to total output, offering a more comprehensive set to test exchange rate disconnect. Specifically, eleven out of thirty countries in Tables 1 and 11 have mean import-to-GDP ratios greater than 35%.

 $<sup>^{12}</sup>$  For each country, from here on, I use as a proxy for the amount of international trade its mean import-to-GDP ratio, for the corresponding time period in Table 10 in Appendix A.2, since it is the value to calibrate the openness-to-international-trade parameter  $\gamma$  in the theoretical model of Section 3. The mean import-to-GDP ratios of Japan, Korea, New Zealand, Sweden, the United Kingdom, and the United States, reported in Table 4 of Itskhoki and Mukhin 2021, are 11.5%, 33.4%, 22.8%, 33%, 24.4%, and 12.1% respectively.

#### 2.2 Exchange Rate Disconnect across Exchange-Rate Regimes

A strand of literature, dating back to Friedman (1953), evaluates the effects of different exchange-rate regimes and asks one of the enduring questions in international macroeconomics and finance: what are the effects of different exchange-rate regimes? Surprisingly, though, it examines principally the breakdown of the Bretton Woods system in 1973, a break in the US exchange-rate regime, and neglects other, similar natural experiments. Figure 2 overcomes this lack of natural experiments, summarizing the empirical results for all the thirty countries and all the exchangerate regime breaks identified by the heteroskedasticity-break in Section 2.1.

Panel (a) of Figure 2 plots annualized standard deviations of real exchange rates in logarithmic difference,  $\sigma(\Delta y_t)$ , against annualized standard deviations of real output in logarithmic difference,  $\sigma(\Delta q_t)$ . These annualized standard deviations are computed across the exchange-rate regimes; the standard deviations are in red (circles) for the pegged regimes and in blue (triangles) for the floating regimes. It is easy to see that when moving from pegged to floating regimes, the volatility of real exchange rates systematically increases for all the studied countries.<sup>13</sup>

But it is not obvious what happens to output volatility when moving from pegged to floating regimes: for some countries, output volatility increases (for instance, Greece [GRC]); for others, it decreases (for instance, Brazil [BRA]). To offer a more systematic answer, Panel (b) of Figure 2 reports in green, country by country, the differences in  $\sigma(\Delta y_t)$  across exchange-rate regimes ( $\Delta [\sigma(\Delta y_t)]$ ) against the differences in  $\sigma(\Delta q_t)$  across exchange-rate regimes ( $\Delta [\sigma(\Delta y_t)]$ ). Overall, Panel (b) of Figure 2 shows a negative correlation that is not statistically significant.<sup>14</sup>

Panels (c) and (d) of Figure 2 expand on this result by plotting  $\sigma(\Delta q_t)$  and  $\sigma(\Delta y_t)$  against import-to-GDP ratios across exchange-rate regimes. Under the pegged regimes, the standard deviations of  $\Delta q_t$  and  $\Delta y_t$  are in red (circles); under the floating regimes, in blue (triangles). Panels (c) and (d) document that when one orders the countries by import-to-GDP ratio, moving from a pegged to a floating regime increases mean real–exchange-rate volatility (upper part) without changing mean output volatility (lower part). The characterization of exchange-rate regimes documents that exchange-rate regime breaks are associated with large changes in the volatility of real exchange rates. This result can also be seen in Panel (c) of Figure 2, where we see that moving from pegged to floating regimes increases the mean standard deviation of the real exchange rate by about 350%, from 2.389 to 8.351.

However, this result makes the finding of Panel (d) of Figure 2 much more puzzling with respect to the US economy, which is represented by the leftmost two points: not only does moving from pegged to floating not change the mean standard deviation of real output across regimes, but it does not systematically increase output volatility in economies for which imports are relatively small compared to total output (those in the center and on the left).

<sup>&</sup>lt;sup>13</sup>Here, in order to match the quarterly frequency of the real macro variables, I identify the exchange-rate regime breaks by applying the heteroskedasticity-break test, developed by Lavielle (1999) and Lavielle and Moulines (2000), to the first difference of the logarithm of the quarterly real exchange rate. Quarterly time-series data on real output, consumption, investment, and net exports come from the Organisation for Economic Co-operation and Development's OECD.Stat.

<sup>&</sup>lt;sup>14</sup>The coefficient of the OLS regression of  $\Delta [\sigma(\Delta y_t)]$  on  $\Delta [\sigma(\Delta q_t)]$  is -0.062 and the 95% confidence interval, using heteroskedasticity-robust standard errors, is [-0.311, 0.188] (the p-value of the test, under the null hypothesis of an OLS coefficient equal to zero, is 0.616).

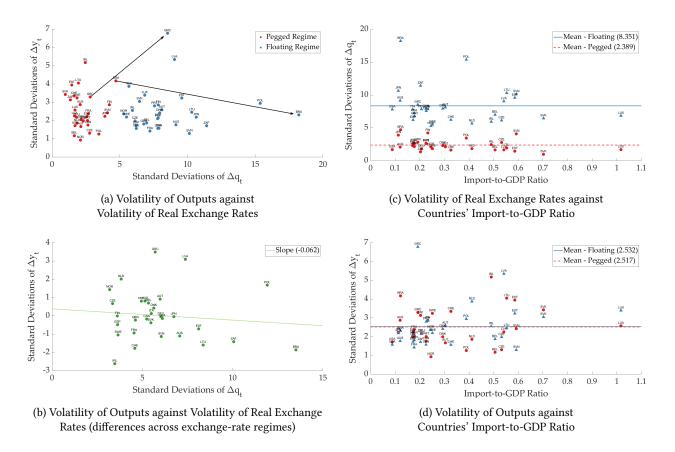


Figure 2: Volatility of Real Exchange Rates and Volatility of Outputs across Exchange-Rate Regimes

*Notes:* The annualized standard deviations are in red (circles) under the pegged regimes and in blue (triangles) under the floating regimes; the differences in the annualized standard deviations across regimes are in green. *Sources:* The Bank of Italy's Exchange Rates Portal, the International Monetary Fund's Direction of Trade Statistics and International Financial Statistics, and the Organisation for Economic Co-operation and Development's OECD.Stat.

Moreover, Table 2 reports the OLS coefficients of the regression of  $\sigma(\Delta q_t)$  on import-to-GDP ratio and the regression of  $\sigma(\Delta y_t)$  on import-to-GDP ratio across exchange-rate regimes. It formally shows that there is no statistically significant correlation between the volatilities of real exchange rates (nor real output) and countries' import-to-GDP ratio across exchange-rate regimes. Countries experience exchange-rate regime breaks, increasing the volatility of their real exchange rates and hence real shocks to their economies, but do not display systematically increased volatility in their real output; additionally, I find no statistically significant correlation between the volatilities of real exchange rates (nor output) and countries' amount of trade with the rest of the world in either regime (Table 2).

Finally, Table 3 provides some additional details by including other real macro variables: consumption ( $\Delta c_t$ ), investment ( $\Delta z_t$ ), and net exports ( $\Delta nx_t$ ). Under the pegged regimes, the mean volatility of the real exchange rate is low and at the same order of magnitude as real output's mean volatility, but there is a disconnect under the floating regimes: the floating-pegged ratio for the real exchange rate is about 3.5, but the ratio is around 1 for all the other real macro variables.

Exchange-Rate Regime	$\sigma(\Delta q_t)$	$\sigma(\Delta y_t)$
Pegged Regime	-1.260 [-2.767, 0.246]	0.721 [-0.776, 2.219]
Floating Regime	-2.000 [-6.082, 2.083]	1.324 [-0.282, 2.930]

Table 2: Relationship between Import-to-GDP Ratio andVolatilities across Exchange-Rate Regimes

Notes: The second column reports the OLS coefficients of the regression of annualized standard deviations of  $\Delta q_t$  on import-to-GDP ratio across exchange-rate regimes; the third column reports the OLS coefficients of the regression of annualized standard deviations of  $\Delta y_t$  on import-to-GDP ratio across exchange-rate regimes; 95% confidence intervals, using heteroskedasticity-robust standard errors, are in square brackets, and the p-values of the test, under the null hypothesis of an OLS coefficient equal to zero, are 0.098 [pegged regime /  $\sigma(\Delta q_t)$ ], 0.322 [pegged regime /  $\sigma(\Delta q_t)$ ], 0.102 [floating regime /  $\sigma(\Delta y_t)$ ].

Exchange-Rate Regime	$\sigma(\Delta q_t)$	$\sigma(\Delta y_t)$	$\sigma(\Delta c_t)$	$\sigma(\Delta z_t)$	$\sigma(\Delta n x_t)$
Pegged Regime	2.389	2.517	2.320	8.904	3.844
	[2.051, 2.726]	[2.146, 2.889]	[1.875, 2.766]	[5.308, 12.500]	[2.975, 4.713]
Floating Regime	8.351	2.532	2.806	7.996	4.231
	[7.301, 9.401]	[2.099, 2.965]	[2.257, 3.356]	[6.533, 9.458]	[3.592, 4.872]
Floating-Pegged Ratio	3.5	1.0	1.2	0.9	1.1

Table 3: Volatilities across Exchange-Rate Regimes

*Notes:* The table reports the mean annualized standard deviations of real macro variables across exchange-rate regimes; 95% confidence intervals, using heteroskedasticity-robust standard errors, are in square brackets, and the p-values of the test, under the null hypothesis of equal means across exchange-rate regimes, are respectively 0.000, 0.958, 0.165, 0.635, and 0.466.

Thus, the second main empirical result of the paper is that exchange rate disconnect remains persistent across exchange-rate regimes, even when countries for which imports, compared to total output, are larger than the United States are studied. The above patterns of change in the volatilities of the real exchange rate and other real macro variables motivate my theoretical analysis in the next section, which aims to resolve exchange rate disconnect without relying on the openness of a country to international trade.

# **3** Theoretical Framework

My model builds on an international real business cycle model with productivity and financial shocks, and it includes three crucial features: imperfect international financial markets (Gabaix and Maggiori 2015), deviations from the law of one price (in the form of variable markups and pricing to market), and exporter-importer firms (Amiti, Itskhoki, and Konings 2014). Section 3.1 illustrates the model. Sections 3.2 explains how resolving exchange rate disconnect requires that exporters simultaneously be intensive importers. In Section 3.3, I complement the model-based analysis with the quantitative results from the calibration.

#### 3.1 Model

Time is discrete and runs forever: t = 0, 1, 2, .... There are two countries—home (France) and foreign (Belgium, denoted with an asterisk)—each with its own nominal unit of account in which local prices are quoted. The nominal exchange rate  $\mathcal{E}_t$  is the price of Belgian francs in French francs: an increase in  $\mathcal{E}_t$  corresponds to a nominal devaluation of the home currency (the French franc). The real exchange rate,  $\mathcal{Q}_t \equiv (P_t^* \mathcal{E}_t)/P_t$ , is the relative consumer price level in the two countries, with  $P_t^*$  being the consumer price index in the foreign country and  $P_t$  being the consumer price index in the home currency. An increase in  $\mathcal{Q}_t$  corresponds to a real depreciation of the home currency. The economy of each country is populated by households, two types of firms (domestic firms and exporter-importer firms), and a government.

The countries are symmetric with the exception of their exchange-rate regime: the foreign country always conducts its monetary policy according to a Taylor rule by targeting inflation (a floating regime), while the home country conducts its monetary policy according to a Taylor rule that switches from targeting the nominal exchange rate (a pegged regime) to targeting inflation (a floating regime). In the following description, I focus on the home country.

#### 3.1.1 The Home Country

**Households.** There is a continuum of identical households of measure 1. The representative household solves a consumption-savings problem, maximizing its discounted expected utility over final consumption  $C_t$  and labor  $L_t$ :

$$\max_{\{C_t, L_t, Z_t, B_{t+1}\}_{t=0}^{\infty}} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left( \frac{1}{1-\sigma} C_t^{1-\sigma} - \frac{1}{1+\varphi} L_t^{1+\varphi} \right)$$

Here,  $\beta$  is the household discount factor,  $\sigma$  is the relative-risk-aversion parameter, and  $\varphi$  is the inverse Frisch elasticity of labor supply, subject to the following budget constraint:

$$P_t C_t + P_t Z_t + \frac{B_{t+1}}{R_t} \le W_t L_t + R_t^K K_t + B_t + \Pi_{Dt} + \Pi_{Et}.$$

Here,  $P_t$  is the consumer price index,  $Z_t$  is the gross investment in the capital stock  $K_t$ ,  $B_t$  is the quantity of the riskfree bond paying out one unit of the home currency at time t,  $R_t$  is the gross nominal interest rate,  $W_t$  is the nominal wage rate,  $R_t^K$  is the nominal rental rate of capital,  $\Pi_{Dt}$  and  $\Pi_{Et}$  are respectively the profits from the domestic firms and the exporter-importer firms. Here, I assume that the representative household in the home country trades only home-currency bonds and owns only home domestic firms and exporter-importer firms.

The within-period consumption expenditure  $P_tC_t$ , between the home good  $C_{Ht}$  and the foreign good  $C_{Ft}$ , is allocated to minimize expenditure on final consumption  $C_t$ :

$$P_t C_t = \int_0^1 \left[ P_{Ht}(i) C_{Ht}(i) + P_{Ft}(i) C_{Ft}(i) \right] di.$$

Here,  $P_{Ht}$  and  $P_{Ft}$  are the home-currency prices of the home and foreign goods. Final consumption  $C_t$  is implicitly defined by the Kimball (1995) aggregator as follows:

$$\int_0^1 \left[ (1-\gamma)g\left(\frac{C_{Ht}(i)}{(1-\gamma)C_t}\right) + \gamma g\left(\frac{C_{Ft}(i)}{\gamma C_t}\right) \right] di = 1.$$

Here,  $\gamma$  is the openness-to-international-trade parameter and the function  $g(\cdot)$  is increasing and concave with  $-g''(1) \in (0,1)$  and g(1) = g'(1) = 1. This minimization results in the following demand schedules:

$$C_{Ht}(i) = (1 - \gamma)h\left(\frac{P_{Ht}(i)}{\mathcal{P}_t}\right)C_t \quad \text{and} \quad C_{Ft}(i) = \gamma h\left(\frac{P_{Ft}(i)}{\mathcal{P}_t}\right)C_t$$

Here, the function  $h(\cdot) = g'^{-1}(\cdot)$  and controls the curvatures of the demand schedules.<sup>15</sup>

<sup>&</sup>lt;sup>15</sup>In this setting, the point elasticity  $\theta = -h'(1)$ , whereas the constant-elasticity-of-substitution aggregator, with elasticity of substitution  $\theta$ , is a special case of the Kimball (1995) aggregator when  $g(x) = 1 + \frac{\theta}{\theta - 1} \left( x^{1 - \frac{1}{\theta}} - 1 \right)$ .

The consumer price index  $P_t$  and the auxiliary variable  $\mathcal{P}_t$  are implicitly defined by the consumption-expenditure equation and by the Kimball (1995) aggregator, after substituting the home demand schedules:

$$P_t = \int_0^1 \left[ (1 - \gamma) P_{Ht}(i) h\left(\frac{P_{Ht}(i)}{\mathcal{P}_t}\right) + \gamma P_{Ft}(i) h\left(\frac{P_{Ft}(i)}{\mathcal{P}_t}\right) \right] di,\tag{1}$$

$$\int_{0}^{1} \left\{ (1-\gamma)g\left[h\left(\frac{P_{Ht}(i)}{\mathcal{P}_{t}}\right)\right] + \gamma g\left[h\left(\frac{P_{Ft}(i)}{\mathcal{P}_{t}}\right)\right] \right\} di = 1.$$
<sup>(2)</sup>

 $Z_t$  accumulates according to the following rule–quadratic capital adjustment costs–with depreciation  $\delta$  and capital adjustment cost  $\kappa$ :

$$K_{t+1} = (1-\delta)K_t + \left[Z_t - \frac{\kappa}{2} \frac{(\Delta K_{t+1})^2}{K_t}\right].$$

Gross investment  $Z_t$  is a bundle of domestic and foreign varieties, as final consumption  $C_t$ , aggregated according to an analogous Kimball (1995) aggregator and demanded according to analogous demand schedules.

**Domestic firms.** There is a continuum of identical domestic firms of measure 1. The representative domestic firm *i* produces using a Cobb-Douglas technology with labor  $L_{Dt}$ , capital  $K_{Dt}$ , and intermediate inputs  $X_{Dt}$ :

$$Y_{Ht} = \left(e^{a_t} K_{Dt}^{\vartheta} L_{Dt}^{1-\vartheta}\right)^{1-\phi} X_{Dt}^{\phi}.$$

Here,  $a_t$  is the logarithm of total factor productivity, which follows an AR(1) process:

$$a_t = \rho_a a_{t-1} + \sigma_a \epsilon_t^a, \qquad \epsilon_t^a \sim \mathcal{N}(0, 1).$$

Here, the persistent parameter  $\rho_a \in [0, 1]$  and the volatility of the innovation  $\sigma_a \ge 0$ . The intermediate input  $X_{Dt}$  is a bundle of domestic and foreign varieties, like final consumption  $C_t$  and gross investment  $Z_t$ , aggregated according to an analogous Kimball (1995) aggregator and demanded according to analogous demand schedules.

The associated marginal cost of production for the domestic firm is

$$MC_{Dt} = \frac{1}{\varpi} \left[ e^{-a_t} R_t^{K^{\vartheta}} W_t^{1-\vartheta} \right]^{1-\phi} P_t^{\phi}, \quad \text{where} \quad \varpi \equiv \phi^{\phi} \left[ (1-\phi) \vartheta^{\vartheta} (1-\vartheta)^{1-\vartheta} \right]^{1-\phi}.$$

In serving the home market, the domestic firm maximizes profits,

$$\Pi_{Dt}(i) = (P_{Ht}(i) - MC_{Dt}) Y_{Ht}(i),$$

by optimally setting  $P_{Ht}(i)$ .

Thanks to the Kimball (1995) aggregator, such profit maximization results in variable-markup pricing with a common price across all domestic firms *i*:

$$P_{Ht}(i) = P_{Ht} = \mu \left(\frac{P_{Ht}}{\mathcal{P}_t}\right) M C_{Dt}.$$
(3)

Here, the markup function  $\mu(x) = \frac{-\frac{\partial \ln h(x)}{\ln x}}{-\frac{\partial \ln h(x)}{\ln x} - 1}$  is derived from the demand schedules of  $C_t$ ,  $K_t$ , and  $X_t$  in the home country. The aggregate profits,  $\Pi_{Dt} = \int_0^1 \Pi_{Dt}(i) di$ , are distributed to the households.

**Exporter-importer firms.** There is a continuum of exporter-importer firms of measure 1. The representative exporter-importer firm j still produces using a Cobb-Douglas technology with labor  $L_{Et}$ , capital  $K_{Et}$ , and intermediate inputs  $X_{Et}$  but also directly imports intermediate inputs  $E_{Ft}^*$ , priced in the foreign currency, from the foreign country:

$$Y_{Ht}^{*} = \left[ \left( e^{a_{t}} K_{Et}^{\vartheta} L_{Et}^{(1-\vartheta_{t})} \right)^{1-\phi} X_{Et}^{\phi} \right]^{1-\phi^{c}} \left( E_{Ft}^{*} \right)^{\phi^{c}}.$$

Given the foreign-currency price of the foreign good  $P_{Ft}^*$ , the associated marginal cost of production for the exporter-importer firm is

$$MC_{Et} = \frac{1}{\varpi^e} \left\{ \left[ e^{-a_t} R_t^{K\vartheta} W_t^{1-\vartheta} \right]^{1-\phi} P_t^{\phi} \right\}^{1-\phi^e} \left( \mathcal{E}_t P_{Ft}^* \right)^{\phi^e}, \text{ where}$$
$$\varpi^e \equiv \phi^{e\phi^e} \left\{ (1-\phi^e) \phi^{\phi} \left[ (1-\phi) \vartheta^{\vartheta} (1-\vartheta)^{1-\vartheta} \right]^{1-\phi} \right\}^{1-\phi^e}.$$

In serving the foreign market, the exporter-importer firm maximizes profits,

$$\Pi_{Et}(j) = \left(P_{Ht}^*(j)\mathcal{E}_t - MC_{Et}\right)Y_{Ht}^*(j),$$

by optimally setting  $P_{Ht}^*(j)$ .

Thanks to the Kimball (1995) aggregator, such profit maximization results in variable-markup pricing with a common price across all exporter-importer firms j:

$$P_{Ht}^*(j) = P_{Ht}^* = \mu\left(\frac{P_{Ht}^*}{\mathcal{P}_t^*}\right) \frac{MC_{Et}}{\mathcal{E}_t}.$$
(4)

Here, the markup function  $\mu(x) = \frac{-\frac{\partial \ln h(x)}{2}}{-\frac{\partial \ln h(x)}{\ln x} - 1}$  is derived from the demand schedules of  $C_t^*$ ,  $K_t^*$ , and  $X_t^*$  in the foreign country. The aggregate profits,  $\Pi_{Et} = \int_0^1 \Pi_{Et}(j) dj$ , are distributed to the households.

**Government in the home country.** The fiscal authority is fully passive, in the sense that I abstract from government spending and taxation, whereas the monetary authority conducts monetary policy according to the following Taylor rule:

$$i_t = \rho_i i_{t-1} + (1 - \rho_i) [\omega_\pi \pi_t + \omega_e (e_t - \bar{e})].$$

Here,  $i_t = ln(R_t)$ ,  $\bar{e}$  is the logarithm of the targeted nominal exchange rate,  $0 \ge \rho_i \le 1$ ,  $\omega_\pi > 1$ , and  $\omega_e \ge 0$ . The parameter  $\rho_i$  represents interest rate smoothing in the monetary-policy rule, whereas the parameters  $\omega_\pi$  and  $\omega_e$  respectively represent the weights of the two monetary-policy objectives, inflation targeting and nominal-exchangerate targeting. When  $\omega_e = 0$ , the monetary authority implements a floating regime; when  $\omega_e > 0$ , a pegged regime.

#### 3.1.2 The Foreign Country

The foreign country is fully symmetric to the home country except that the monetary authority conducts monetary policy according to the following Taylor rule:

$$i_t^* = \rho_{i^*} i_{t-1}^* + (1 - \rho_{i^*}) \omega_{\pi^*} \pi_t^*.$$

Here,  $0 \ge \rho_{i^*} \le 1$  and  $\omega_{\pi^*} > 1$ . The parameter  $\rho_{i^*}$  represents interest rate smoothing in the monetary-policy rule. Unlike in the home country, the monetary authority always implements a floating regime.

#### 3.1.3 International Financial Markets

The international financial markets are segmented since the home and foreign households cannot directly trade any bonds with each other. Their international financial positions are intermediated by a unit mass of global financial firms, each managed by a financier.

The representative financier solves the following constrained problem:

$$\max_{Q_t} V_t = \mathbb{E}_t \left[ \beta(R_t - R_t^* \frac{\mathcal{E}_{t+1}}{\mathcal{E}_t}) \right] Q_t, \quad \text{subject to} \quad V_t \ge \Gamma_t \frac{Q_t^2}{\mathcal{E}_t}.$$

Here,  $Q_t$  is the balance-sheet position of the financier, in French francs, and  $\Gamma_t = \xi [\operatorname{Var}_t(\mathcal{E}_{t+1})]^{\alpha}$ , with  $\xi \ge 0$  and  $\alpha \ge 0$ .  $\Gamma_t$  represents the financiers' risk-bearing capacity. For simplicity of the model, I assume that financiers rebate their profits and losses to the foreign households, not the home ones.

I introduce exogenous financial shocks to the international financial markets only in the linearized version of the model, without taking a stance on their microfoundation, as they can be equally generated from exogenous portfolio flows of the households, as in Gabaix and Maggiori (2015); from noise traders, as in Itskhoki and Mukhin (2021, 2025); or from biased exchange-rate expectations, as in Jeanne and Rose (2002).

An important assumption of the model is that the representative household in the home (foreign) country trades only home-currency (foreign-currency) bonds and owns only home (foreign) domestic firms and exporter-importer firms. As a consequence, the home (foreign) country is borrowing and lending in its own currency only. One can alternatively write the model with a representative household (and representative domestic and exporter-importer firms) which can borrow in the foreign currency, stipulating an additional channel of transmission of nominal exchange-rate fluctuations in the same fashion as Fukui, Nakamura, and Steinsson (2025). European countries up to the beginning of the nineties had tight capital control restrictions on foreign currency exposures, so I take this simpler formulation.<sup>16</sup>

#### 3.1.4 Market Clearing

Labor market. In the home country, nominal wage rate  $W_t$  adjusts to clear the labor market, such that the labor supply of households

$$C_t^{\sigma} L_t^{1/\varphi} = \frac{W_t}{P_t}$$

satisfies the labor demand from domestic firms and exporter-importer firms

$$W_t L_t = W_t L_{Dt} + W_t L_{Et} = (1 - \phi)(1 - \vartheta) M C_{Dt} Y_{Ht}, + (1 - \phi^e)(1 - \phi)(1 - \vartheta) M C_{Et} Y_{Ht}^*$$

**Capital market.** In the home country, nominal rental rate of capital  $R_t^K$  adjusts to clear the capital market, such that the capital supply of households:

$$\left(1+\kappa\frac{\Delta K_{t+1}}{K_t}\right)C_t^{-\sigma} = \beta \mathbb{E}_t \left\{ \left(C_{t+1}^{-\sigma}\right) \left[\frac{R_{t+1}^K}{P_{t+1}} - \delta + \left(1+\kappa\frac{\Delta K_{t+2}}{K_{t+1}}\right) + \frac{\kappa}{2}\frac{\left(\kappa\frac{\Delta K_{t+2}}{K_{t+1}}\right)^2}{2\kappa}\right] \right\}$$

satisfies the capital demand from domestic firms and exporter-importer firms

$$R_{t}^{K}K_{t} = R_{t}^{K}K_{Dt} + R_{t}^{K}K_{Et} = (1-\phi)\vartheta MC_{Dt}Y_{Ht} + (1-\phi^{e})(1-\phi)\vartheta MC_{Et}Y_{Ht}^{*}.$$

**Goods market.** In the home country, clearing the goods market requires that total production by the home domestic firms and exporter-importer firms is split between supply to the home and foreign markets respectively and satisfies the demand in each market:

$$Y_t = Y_{Ht} + Y_{Ht}^*,$$

<sup>&</sup>lt;sup>16</sup>Akinci, Şebnem Kalemli-Özcan, and Queralto (2023) also emphasizes intermediation frictions in the presence of long-lived financial intermediaries that face leverage constraints.

$$Y_{Ht} = C_{Ht} + X_{Ht} + Z_{Ht} + E_{Ht} = (1 - \gamma)h\left(\frac{P_{Ht}}{\mathcal{P}_t}\right)[C_t + X_t + Z_t] + E_{Ht}, \text{ and}$$
$$Y_{Ht}^* = C_{Ht}^* + X_{Ht}^* + Z_{Ht}^* = \gamma h\left(\frac{P_{Ht}^*}{\mathcal{P}_t^*}\right)[C_t^* + X_t^* + Z_t^*].$$

Finally, I derive the home country's budget constraint:

$$\frac{B_{t+1}}{R_t} - B_t = NX_t \quad \text{with} \quad NX_t = (\mathcal{E}_t P_{Ht}^* Y_{Ht}^* + P_{Ht} E_{Ht}) - (P_{Ft} Y_{Ft} + \mathcal{E}_t P_{Ft}^* E_{Ft}^*).$$

Here,  $NX_t$  are net exports in units of the home currency.

Net exports contain two extra terms, relative to a model without exporter-importer firms: the directly imported intermediate inputs of the foreign exporter-importer firm  $(E_{Ht})$  and the directly imported intermediate inputs of the home exporter-importer firm  $(E_{Ft}^*)$ , the prices of which are  $P_{Ht}$  and  $P_{Ft}^*$ , respectively.

**International financial markets.** Clearing the international financial markets requires that the balance sheet position of the financiers in French francs  $Q_t$  equals  $B_t$  and the balance sheet position of the financiers in Belgian francs  $Q_t^*$  equals  $B_t^*$ .

#### 3.1.5 Equilibrium Definition and Model Solution

In Appendix A.3.1.5, I define an equilibrium in the nonlinear model. I solve the model by logarithmic linearization around a symmetric steady state with steady-state markup  $\bar{\mu} = 1$  and, from now on, I denote all the expressions in terms of deviations from the symmetric steady-state equilibrium; for example,  $y_t \equiv \ln(Y_t) - \ln(\bar{Y})$ .

#### 3.2 Exporter-Importer Firms Resolving Exchange Rate Disconnect

Two equations characterize the linearized model around a symmetric steady state: the modified UIP condition in the international financial markets, and the home flow budget constraint.

The logarithmic linearization of the equilibrium condition in the international financial markets results in the following modified UIP condition, which is subject to exogenous financial shocks:

$$i_t - i_t^* - \mathbb{E}_t \Delta e_{t+1} = \chi_1 \psi_t - \chi_2 b_{t+1}.$$
(5)

Here,  $b_{t+1} = B_{t+1}/\bar{Y}$ ,  $\chi_1 = \Gamma$ , and  $\chi_2 = \Gamma \beta \bar{Y}$ . The exogenous financial shocks  $\psi_t$  follow an AR(1) process:

$$\psi_t = \rho_{\psi} \psi_{t-1} + \sigma_{\psi} \epsilon_t^{\psi}, \qquad \epsilon_t^{\psi} \sim \mathcal{N}(0, 1).$$

The persistent parameter  $\rho_{\psi} \in [0, 1]$ , and the volatility of the innovation  $\sigma_{\psi} \ge 0$ .

When the financiers' risk-bearing capacity  $\Gamma = 0$ , they can absorb any imbalances, which results in no deviation from the UIP condition;  $i_t - i_t^* - \mathbb{E}_t \Delta e_{t+1} = 0$ . The higher the  $\Gamma$ -that is, the lower the financiers' risk-bearing capacity-the more segmented the international financial markets. For  $0 < \Gamma < \infty$ , the model endogenously generates UIP deviations.<sup>17</sup>

The logarithmic linearization of the home country's flow budget constraint results in the following equation:

$$nx_t = (1 - \phi^e)\tilde{\gamma}e_t + \tilde{\gamma}(y_{Ht}^* - y_{Ft} + p_{Ht}^* - p_{Ft}) + \phi^e\tilde{\gamma}(e_{Ht} - e_{Ft}^* + p_{Ht} - p_{Ft}^*).$$
(6)

Here,  $nx_t = \frac{NX_t}{\bar{Y}}$  and  $\tilde{\gamma} \equiv \frac{\gamma}{1+\phi^e\gamma}$ .

Thanks to the inclusion of exporter-importer firms, I can state the following proposition on how to resolve exchange rate disconnect under the floating regime.<sup>18</sup> I relegate the quantitative analysis to Section 3.3.

#### **PROPOSITION.**

Assume that  $\Gamma > 0$  and  $\omega_e = 0$ . For any value of  $\gamma$ ,  $c_t - c_t^* = \frac{(1+\varphi)}{1+\varphi\sigma}(a_t - a_t^*)$  if  $\phi^e \to 1$ . **Proof.** See Appendix A.3.2.

**Discussion.** Here, I show how my model's feature contributes to the literature with the aid of three crucial parameters:  $\Gamma$ , the financiers' risk-bearing capacity;  $\gamma$ , the openness-to-international-trade parameter; and  $\phi^e$ , the import intensity of the exporter-importer firms.

Monacelli (2004). If the financiers' risk-bearing capacity  $\Gamma = 0$ , the financiers are able to absorb any imbalances, resulting in no deviation from the UIP condition. The model collapses to a model without financial-market frictions, similar to Monacelli's (2004) model in which the Backus and Smith (1993) condition of efficient international risk sharing holds and the consumption difference across countries co-moves with the real exchange rate. This model outcome is empirically implausible because of the absence of simultaneous structural breaks in the consumptiondifference volatility.<sup>19</sup>

Itskhoki and Mukhin (2021, 2025).  $\Gamma > 0$  with  $\gamma \to 0$  is the solution adopted by Itskhoki and Mukhin (2021, 2025). In this world,  $\phi^e = 0$ , the exporters are not intensive importers, and their production technology is identical to the one of domestic firms. Equation (6) becomes equal to the following:

$$nx_t = \gamma (e_t + y_{Ht}^* - y_{Ft} + p_{Ht}^* - p_{Ft}).$$
<sup>(7)</sup>

 $<sup>^{17}</sup>$ If  $\Gamma \uparrow \infty$ , the financiers are unwilling to absorb any imbalances; that is, they do not take any positions in the international financial markets.  $^{18}$ I state the proposition for the home country; a symmetric one applies for the foreign country.

<sup>&</sup>lt;sup>19</sup>However, if one introduces price stickiness à la Calvo (1983), the model is able to match the Mussa puzzle, the fact that nominal and real exchange rates co-move across exchange-rate regime breaks.

Equation (7) illustrates how the openness-to-international-trade parameter plays a crucial role in isolating the exchangerate volatility in the home economy under the floating regime. This is because if  $\gamma \to 0$ , as is true for the US economy, real macro variables do not react ( $\gamma = 0$  represents complete autarky). As we will see in Section 3.3, this resolution under the floating regime does not work for Belgium, Sweden, South Korea, and the United Kingdom, since real macro variables strongly react when the openness-to-international-trade parameter  $\gamma > 0$ . In the case of the United States with  $\gamma \to 0$ , it is, moreover, unable to capture the muted reaction of exports  $y_{Ht}^*$  and imports  $y_{Ft}$ , taken into account separately, to exchange-rate fluctuations.

*Exporter-importer firms.* Incorporating exporter-importer firms is my main theoretical finding, as it allows me to account for economies for which exports and imports are large compared to total output:  $\Gamma > 0$ ,  $\gamma > 0$ , and  $\phi^e > 0$ .

Under the pegged regimes, the resolution of exchange rate disconnect is straightforward and does not rely on the exporter-importer firms. Suppose that the home country's monetary authority implements a perfect currency board, implying that  $e_t = \bar{e}$  for any t. Then the financiers' risk-bearing capacity  $\Gamma = 0$  and there are no deviations from the UIP condition, so  $i_t - i_t^* - \mathbb{E}_t \Delta e_{t+1} = i_t - i_t^* - \bar{e} + \bar{e} = 0$ . Consequently, real macro variables are not affected by exchange-rate volatility, which is absent because  $e_t = \bar{e}$  for any t, but only by productivity shocks.<sup>20</sup>

Under the floating regimes, the resolution of exchange rate disconnect is more complex and crucially relies on exporter-importer firms. Suppose that the home country's monetary authority implements a fully floating regime such that  $\omega_e = 0$ . Then the financiers' risk-bearing capacity  $\Gamma > 0$ , implying endogenous UIP deviations and a decreasing capacity to bear the risk of an increasing volatility of  $e_t$  because  $\Gamma = \xi [\operatorname{Var}_t(\mathcal{E}_{t+1})]^{\alpha}$ . Now, suppose that  $\phi^e > 0$ , the exporters are intensive importers, and their production technology is very different from the one of the domestic firms, as they largely take advantage of directly imported intermediate inputs. The exporter-importer firms then are playing an active role in isolating the exchange-rate volatility in the home economy, *independently* of the openness-to-international-trade parameter  $\gamma$ . This can be seen in equation (6), in which real macro variables are increasingly muted to the volatility of  $e_t$  for  $\phi^e > 0$  and become completely isolated in the limit as  $\phi^e \to 1$ .<sup>21</sup>

If output is produced by a unique firm that sells in the domestic and foreign markets, the firm has no incentive to specialize its production to serve one of the two markets, in particular the foreign one. So the firm cannot hedge an eventual exchange-rate fluctuation: either it is transmitted to the final consumer through a different price, or it is absorbed through its markup. However, if output is produced by two types of firms, one selling in the domestic market and the other selling in the foreign market, the latter firm—the exporter—has an incentive to specialize its production to serve the foreign market and import a large part of its intermediate inputs from the foreign country. This results in an exporter-importer firm that can hedge the eventual exchange-rate shock, independently of its magnitude, without transmitting it to the rest of the economy.

<sup>&</sup>lt;sup>20</sup>Indeed, the first term on the right-hand side of the home country's flow budget constraint, Equation (6), is a constant.

<sup>&</sup>lt;sup>21</sup>The exporter-importer firms use no local inputs if  $\phi^e = 1$ .

#### 3.3 Calibration

For a transparent comparison between my model with exporter-importer firms and a model with no exporterimporter firms, I follow the assumptions and calibration in Itskhoki and Mukhin (2021), which presents a model without exporter-importers firms. I adopt the same model parameters, as summarized in Table 12 in Appendix A.3.3, with three exceptions: first, I change the openness-to-international-trade parameter  $\gamma$  from 0.07 (the US calibration in Itskhoki and Mukhin 2021) to be consistent with the mean import-to-GDP ratios of several economies—namely, Belgium, Korea, Sweden, and the United Kingdom—for which the mean import-to-GDP ratios are above 22.8%; second, I modify the capital-adjustment-cost parameter  $\kappa$  to match the relative volatility of investment and output,  $std(\Delta z_t)/std(\Delta y_t)$ , whose value is 2.5 as in Itskhoki and Mukhin (2021); third, I choose 0.23 as the value of  $\omega_e$ , the weight of nominal–exchange-rate targeting (in the pegged regime) in the Taylor rule of the home country, following Itskhoki and Mukhin (2025), as Itskhoki and Mukhin (2021) do not analyze the pegged regimes. Lastly, I set  $\phi^e = 0.74$ following the empirical finding in Amiti, Itskhoki, and Konings (2014) that 74% is the ratio between imported inputs and exports for import-intensive exporters.<sup>22</sup>

My model, like the multi-shock version of Itskhoki and Mukhin's (2021) model, features three exogenous shocks for which I need to calibrate the covariance matrix: two country-specific productivity shocks  $(a_t, a_t^*)$  and a financial shock  $(\psi_t)$ . I assume that  $\psi_t$  is orthogonal to  $(a_t, a_t^*)$ , whereas  $a_t$  and  $a_t^*$  have the same variance (that is,  $\sigma_a = \sigma_{a^*}$ ), and a nonzero correlation  $(\rho_{a,a^*})$ . I always choose the relative volatility of the shocks,  $\sigma_a/\sigma_{\psi}$ , to match the Backus-Smith correlation between the United States and the rest of the world,  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , while I always set the cross-country correlation of productivity shocks,  $\rho_{a,a^*}$ , to match the correlation of the United States with the rest of the world,  $corr(\Delta y_t, \Delta y_t^*) = 0.35$ .

#### 3.3.1 Calibration Results

**Floating regime.** I find three main results (see Table 4, Table 5, and Table 7 respectively). First, the real exchange rate is strongly correlated with the nominal exchange rate in both models.

Second, for values of  $\gamma \ge 0.122$ , there is no longer disconnect between exchange rates and other real macro variables in the theoretical model of Itskhoki and Mukhin (2021), whereas my model maintains the disconnect thanks to the exporter-importer firms that actively hedge the exchange-rate fluctuations. Indeed, the muted reaction of real macro variables in the theoretical model of Itskhoki and Mukhin (2021, 2025) arises in a calibration that targets the US economy, a country in which exports and imports are relatively small compared to total output.

<sup>&</sup>lt;sup>22</sup>Remarkably, this represents, at most, a conservative value of  $\phi^e$ , as Amiti, Itskhoki, and Konings (2014) use Belgian firm-product-level data on exports and imports between 2000 and 2008, during which Belgium features a pegged regime under my characterization of exchange-rate regimes. Indeed, if one excludes from the calculation exports and imports to and from the euro area, the ratio between imported inputs and exports for the import-intensive exporters becomes 1.44. However, I set  $\phi^e = 0.74$  in my calibration, as Belgium was still pegged to some countries (for example, Germany, Austria, the Netherlands) under the floating regimes.

Third, I show that the theoretical model of Itskhoki and Mukhin (2021) misses an important feature also for the United States: it is unable to capture the muted reaction of exports or imports to exchange-rate movements when they are considered separately, while I show that my model can capture this. Essentially, the model of Itskhoki and Mukhin (2021) fails because it generates overly volatile exports and imports and only "succeeds" in the aggregate when such variables play a limited role in the overall economy.

Table 4 reports the simulation results, for 10,000 simulations of 120 quarters, and compares the results of my model under the floating regime (that is,  $\omega_e = 0$ ), first, with the results of the authors' preferred version of the Itskhoki and Mukhin (2021) model—the one featuring local currency pricing (LCP) with price and wage stickiness à la Calvo (1983)—and, second, with the results of the Itskhoki and Mukhin (2021) model featuring fully flexible prices and wages, where the currency denomination of exports and imports is irrelevant. I choose values for  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to match  $std(\Delta z_t)/std(\Delta y_t) = 2.5$ ,  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , and  $corr(\Delta y_t, \Delta y_t^*) = 0.35$ , respectively.

In the third column of Table 4, I report the model moments from the US calibration with  $\gamma = 0.07$  in Itskhoki and Mukhin (2021) featuring LCP with price and wage stickiness à la Calvo (1983); in the fourth column, I set the values of  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to target the moments in the Itskhoki and Mukhin (2021) model with  $\gamma = 0.253$ —the half of the average imports-to-GDP ratio of Belgium over the 1960–2019 period—and LCP under price and wage stickiness à la Calvo (1983); in the fifth column, I set the values of  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to target the moments in the Itskhoki and Mukhin (2021) model with  $\gamma = 0.253$ —the half of the values of  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to target the moments in the Itskhoki and Mukhin (2021) model with  $\gamma = 0.253$  and fully flexible prices and wages; in the seventh column, I set the values of  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to target the moments in my model, which does not feature price and wage stickiness, with  $\gamma = 0.253$ . Additionally, I propose a version of my model—in the sixth column of Table 4—that features price and wage stickiness à la Calvo (1983) with the same stickiness parameters of the model in Itskhoki and Mukhin (2021). I do this to make the two models more comparable and to emphasize the pivotal role of exporter-importer firms.

The first result in Table 4 is that both models match strong correlation of the real exchange rate with the nominal exchange rate in all the calibrations. Yet, while for  $\gamma = 0.07$  the Itskhoki and Mukhin (2021) theoretical model can capture the disconnect between the volatility of exchange rates and the other real macro variables, it loses this capability when  $\gamma$  is equal to 0.253. For any of the two calibrations with  $\gamma = 0.253$ , my model performs better than the other in insulating the real macro variables from exchange-rate volatility. This is because of the role of the exporter-importer firms, which actively hedge the exchange-rate fluctuations, independently of the magnitude of shocks, thanks to their amount of directly imported intermediate inputs. Moreover, the sixth and seventh columns of Table 4 show that my model performs well even without price and wage stickiness à la Calvo (1983), which represents another key difference from the Itskhoki and Mukhin (2021) model, the authors' preferred version of which features LCP and price and wage stickiness à la Calvo (1983). Indeed, the stability in quantities and prices in my model endogenously arises as a result of the capacity of exporter-importer firms to be shock absorbers, insulating consumers and domestic firms from nominal exchange fluctuations which are primarily driven by exogenous financial shocks.

However, my conjecture is that this latter result would change in the presence of other additional exogenous shocks.<sup>23</sup>

Table 5 reports the simulation results, for 10,000 simulations of 120 quarters, showing that the model in Itskhoki and Mukhin (2021) is not able to match the disconnect between exchange rates and real macro variables more generally, for economies with average import-to-GDP ratios higher than 22.8% (double the  $\gamma$  parameter in the table). To illustrate this issue, I focus on economies with high import-to-GDP ratios that are discussed by Itskhoki and Mukhin (2021, 2025) and show in Table 5 what would happen in those economies under the Itskhoki and Mukhin (2021) calibration. Hence, Table 5 compares the empirical moments of Korea, Sweden, New Zealand, and the United Kingdom from Table 4 in Itskhoki and Mukhin (2021, p. 2223) with the calibrated ones from the same model.<sup>24</sup> Remarkably, the disconnect between exchange rates and other real macro variables is missing in the calibrations featuring LCP with price and wage stickiness à la Calvo (1983) (upper panel), and also in the calibrations featuring fully flexible prices and wages (lower panel).

Table 6 reports the simulation results, for 10,000 simulations of 120 quarters, performing a sensitivity analysis for different positive values of  $\phi^e$ —namely, 0.37, 0.555, and 0.74—to show that my model performs better than the model in Itskhoki and Mukhin (2021) in matching the disconnect between exchange rates and other real macro variables even for lower values of the import intensity of the exporter-importer firms. Indeed, each of the calibrations of my model in Table 6, that is featuring a positive value of  $\phi^e$ , performs better than the one with  $\phi^e = 0$ . Again, this result remains true in the calibrations featuring LCP with price and wage stickiness à la Calvo (1983) (upper panel), and in the calibrations featuring fully flexible prices and wages (lower panel).

Last, Table 7 reports the simulation results, for 10,000 simulations of 120 quarters, and compares the quantitative results of my model under the floating regimes with the quantitative results of the authors' preferred version of which features LCP and price and wage stickiness à la Calvo (1983), taking into account exports and imports separately for the United States. I again set  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to target the moments in the Itskhoki and Mukhin (2021) model with  $\gamma = 0.07$ . If net exports are decomposed in exports and imports, the openness-to-international-trade parameter  $\gamma$  cannot play a role anymore in the model in isolating the exchange-rate volatility; see equations (6) and (7). Indeed, if one takes them separately, their volatility in the Itskhoki and Mukhin (2021) model has the same order of magnitude of the real exchange rate (see the second and third cells in the third column), a result that is at odds with the empirical evidence (see the second and third cells in the second column). Introducing exporter-importer firms into the model solves this issue, even without modifying the calibration, because it creates a natural hedging mechanism through their directly imported inputs, making real exports and imports insulated to exchange-rate fluctuations.

<sup>&</sup>lt;sup>23</sup>A result in the literature on dynamic stochastic general equilibrium (DSGE) is that price and wage stickiness can improve the quantitative fit when preference, monetary, or investment-specific shocks are incorporated (see, for instance, Smets and Wouters, 2003, 2007 and Justiniano, Primiceri, and Tambalotti, 2010).

<sup>&</sup>lt;sup>24</sup>In this table, following exactly the same approach of Itskhoki and Mukhin (2021, p. 2223-24), I break the symmetry between  $\gamma$  and  $\gamma^*$ , allowing for  $\gamma > \gamma^*$ , and keep all other parameters unchanged, adjusting the relative volatility of shocks to keep the Backus-Smith correlation,  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*)$  equal to -0.4 and the cross-country GDP correlation  $corr(\Delta y_t, \Delta y_t^*)$  equal to 0.35.

**Pegged regime.** Table 8 shows that my model can also accommodate a pegged regime for a value of  $\omega_e = 0.23$ , without recalibrating the covariance matrix of exogenous shocks. This results in decreased output and consumption volatilities relative to the exchange-rate volatility, but the correlation between the nominal and the real exchange rate is still strong, confirming my model's ability to replicate the Mussa puzzle.

However, it looks like the model quantitatively underperforms, in the pegged regime, in replicating the same moments as before.<sup>25</sup> This is because the volatility of the real macro variables is too low, which can be easily understood in light of my discussion in Section 3.2. Under pegged regimes, countries feature only two exogenous shocks—the country-specific productivity shocks  $(a_t, a_t^*)$ —as the financial shock,  $\psi_t$ , is completely absorbed by the financiers, which have full risk-bearing capacity (that is,  $\Gamma = 0$ ) under the pegged regimes.

I can improve on this by adding a third type of shock—a preference shock—to the model, as in Itskhoki and Mukhin (2025), and recalibrating the covariance matrix of exogenous shocks under the floating regime. Nevertheless, as my goal is to explain exchange rate disconnect and the Mussa puzzle, with exporter-importer firms playing a key role in preventing transmission of exchange-rate volatility to the rest of the economy under the floating regime, I do not include preference shocks, as it keeps my model fully comparable with Itskhoki and Mukhin (2021) model.

 $<sup>^{25}</sup>$  This can be seen by looking at  $\sigma(\Delta n x_t)/\sigma(\Delta q_t).$ 

Table	lable 4: Results without and with Exporter-Importer Firms for United States and Belgium	out and with Exp	orter-Import	er Firms for U	Inited States a	and Belgium	
Floating Regime $(\omega_e=0)$		No Expoi	No Exporter-Importer Firms $(\phi^e=0)$	Firms	Exporter-Importer $(\phi^e=0.74)$	er-Importer Firms $(\phi^e=0.74)$	
	US Moments	United States	Belgium	Belgium	Belgium	Belgium	Belgian Moments
		$\gamma=0.07$	$\gamma = 0.253$	$\gamma = 0.253$	$\gamma = 0.253$	$\gamma = 0.253$	
$corr(\Delta e_t,\Delta q_t)$	0.99	1.00	0.99	0.83	1.00	0.99	0.95
$\sigma(\Delta e_t)/\sigma(\Delta g d p_t)$	5.2	3.4	1.0	1.8	1.8	2.1	3.7
$\sigma(\Delta e_t)/\sigma(\Delta c_t)$	6.3	5.8	2.2	2.1	3.6	3.2	4.8
$\sigma(\Delta n x_t)/\sigma(\Delta q_t)$	0.10	0.17	0.60	1.33	0.29	0.27	0.17
Price and Wage Stickiness	I	YES	YES	NO	YES	NO	I
Notes: The US empirical moments in the second column are from Tables 1 and 3 in Itskhoki and Mukhin (2021); the Belgian moments in the seventh column are from Section 2; the model moments for the United States, in the third column, are also from Tables 1 and 3 in Itskhoki and Mukhin (2021). Each cell in the fourth, fifth, and sixth columns of the table is the median value of moments across 10,000 simulations of 120 quarters; I choose $\kappa$ , $\sigma_a$ , and $\rho_{a,a^*}$ to respectively match the targeted moments $std(\Delta z_t)/std(\Delta y_t) = 2.5$ , $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , and $corr(\Delta y_t, \Delta y_t^*) = 0.35$ . In the calibration in the fourth column of the table, I set $\kappa = 5$ , $\sigma_a = 5.24$ , and $\rho_{a,a^*} = 0.41$ to match the targeted moments in the model of Itskhoki and Mukhin (2021) with $\gamma = 0.253$ and price and wage stickiness à la Calvo (1983) into account; in the calibration in the fifth column of the table, I set $\kappa = 22$ , $\sigma_a = 4$ , and $\rho_{a,a^*} = 0.16$ to match the targeted moments in the model of Itskhoki and Mukhin (2021) with $\gamma = 0.253$ and price and wage stickiness à la Calvo (1983) into account; in the calibration in the sixth column, I set $\kappa = 3.5$ , $\sigma_a = 3.45$ , and $\rho_{a,a^*} = 0.38$ to match the targeted moments in the sacount; in the calibration in the sixth column, I set $\kappa = 12$ , $\sigma_a = 3.84$ , and $\rho_{a,a^*} = 0.38$ to match the targeted moments in my model with exporter-importer firms with $\gamma = 0.253$ and price and wage stickiness à la Calvo (1983) into account. The last row of the table indicates whether the model is calibrated taking price and wage stickiness à la Calvo (1983) into account. (1983) into account.	n the second column the United States, in the value of moments an $\Delta q_t$ , $\Delta c_t - \Delta c_t^*$ ) = eted moments in the tof the table, I set $\kappa$ : of the table, I set $\kappa$ : are a sickiness à la ( model with exporter $a = 3.84$ , and $\rho_{a,a^*}$ or (1983) into account	n are from Tables 1 ne third column, are cross 10,000 simulat $\alpha = -0.4$ , and $corr(\Delta x)$ model of Itskhoki ar = 22, $\sigma_a = 4$ , and $\rho$ Calvo (1983) into acc -importer firms with $\alpha = 0.38$ to match th t. The last row of th	and 3 in Itskhok also from Tables ions of 120 quar $\mu$ , $\Delta y_t^*$ ) = 0.37 $a, a^* = 0.16$ to 1 $a, a^* = 0.16$ to 1 ount; in the calil $1\gamma = 0.253$ and ne targeted mom e table indicates	i and Mukhin (2 1 and 3 in Itskhe ters; I choose $\kappa$ , i. In the calibrati with $\gamma = 0.253$ match the target price and wage : price and wage : ents in my mode	2021); the Belgiar oki and Mukhin ( $i \sigma_a$ , and $\rho_a$ , $a^*$ to on in the fourth of and price and we ad noments in the ed noments in the column, I set the column, I set stickiness à la Ca el with exporter-i del is calibrated	1 moments in the 2021). Each cell in 2021). Each cell in column of the tabl age stickiness à la age stickines à la age stickines à la stickines à la $\kappa = 3.5, \sigma_a = 3$ lvo (1983) into aco mporter firms with taking price and b	ts in the seventh column are from the cell in the fourth, fifth, and sixth ively match the targeted moments f the table, I set $\kappa = 5$ , $\sigma_a = 5.24$ , ness à la Calvo (1983) into account; of Itskhoki and Mukhin (2021) with $\sigma_a = 3.45$ , and $\rho_{a,a^*} = 0.74$ to ) into account; in the calibration in firms with $\gamma = 0.253$ and without ice and wage stickiness à la Calvo

Table 4: Results without and with Exporter-Importer Firms for United States and Belgium

	No Exporter-Importer Firms $(\phi^e=0)$							
	New Zea	aland	United Ki	ngdom	Swed	en	South K	Corea
	$\gamma = 0.$	114	$\gamma = 0.$	122	$\gamma = 0.$	165	$\gamma = 0.$	167
	Moments	Model	Moments	Model	Moments	Model	Moments	Model
$autocorr(q_t)$	0.96	0.91	0.93	0.91	0.97	0.91	0.92	0.91
$\sigma(\Delta q_t)/\sigma(\Delta e_t)$	1.01	0.99	1.04	0.98	0.99	0.98	0.95	0.98
$corr(\Delta q_t, \Delta c_t - \Delta c_t^*)$	0.01	-0.4	-0.03	-0.4	-0.17	-0.4	-0.50	-0.4
$\sigma(\Delta e_t)/\sigma(\Delta g dp_t)$	2.1	3.6	4.9	2.3	2.9	1.7	3.3	1.7
$\sigma(\Delta n x_t) / \sigma(\Delta q_t)$	0.26	0.28	0.16	0.30	0.25	0.41	0.24	0.42
Price and Wage Stickiness	_	YES	_	YES	_	YES	_	YES
$autocorr(q_t)$	0.96	0.92	0.93	0.92	0.97	0.92	0.92	0.92
$\sigma(\Delta q_t)/\sigma(\Delta e_t)$	1.01	0.91	1.04	0.90	0.99	0.86	0.95	0.86
$corr(\Delta q_t, \Delta c_t - \Delta c_t^*)$	0.01	-0.4	-0.03	-0.4	-0.17	-0.4	-0.50	-0.4
$\sigma(\Delta e_t)/\sigma(\Delta g dp_t)$	2.1	2.4	4.9	2.49	2.9	2.1	3.3	2.0
$\sigma(\Delta n x_t) / \sigma(\Delta q_t)$	0.26	0.42	0.16	0.46	0.25	0.64	0.24	0.65
Price and Wage Stickiness	_	NO	_	NO	_	NO	_	NO

Table 5: Results without Exporter-Importer Firms for Countries with Mean Import-to-GDP Ratios Higher than 22.8%

Notes: The empirical moments in the second, fourth, sixth, and eightieth columns are from Table 4 in Itskhoki and Mukhin (2021); the model moments for New Zealand taking price and wage stickiness à la Calvo (1983) into account, in the third column of the upper panel, are also from Table 4 in Itskhoki and Mukhin (2021); the model moments for New Zealand without taking price and wage stickiness à la Calvo (1983) into account, in the third column of the upper panel, are also from Table 4 in Itskhoki and Mukhin (2021); the model moments for New Zealand without taking price and wage stickiness à la Calvo (1983) into account, in the third column of the lower panel, are the median values of moments across 10,000 simulations of 120 quarters. Each cell in the fifth, seventh, and ninetieth columns of the table is the median value of moments across 10,000 simulations of 120 quarters; I choose  $\sigma_a$  and  $\rho_{a,a^*}$  to respectively match the targeted moments  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , and  $corr(\Delta y_t, \Delta y_t^*) = 0.35$ . In calibration for New Zealand in the lower panel, I set  $\gamma = 0.114$ ,  $\gamma^* = 0.0005$ ,  $\kappa = 6.8$ ,  $\sigma_a = 3.45$ , and  $\rho_{a,a^*} = 0.48$ ; in calibration for the United Kingdom, in the upper panel, I set  $\gamma = 0.122$ ,  $\gamma^* = 0.005$ ,  $\kappa = 6.8$ ,  $\sigma_a = 3.18$ , and  $\rho_{a,a^*} = 0.67$ ; in calibration for the United Kingdom, in the upper panel, I set  $\gamma = 0.122$ ,  $\gamma^* = 0.005$ ,  $\kappa = 6.8$ ,  $\sigma_a = 3.28$ , and  $\rho_{a,a^*} = 0.50$ ; in the calibration for Sweden, in the upper panel, I set  $\gamma = 0.165$ ,  $\gamma^* = 0.0015$ ,  $\kappa = 6.8$ ,  $\sigma_a = 3.96$ , and  $\rho_{a,a^*} = 0.73$ ; in the calibration for Sweden, in the lower panel, I set  $\gamma = 0.167$ ,  $\gamma^* = 0.0025$ ,  $\kappa = 6.8$ ,  $\sigma_a = 3.98$ , and  $\rho_{a,a^*} = 0.73$ ; in the calibration for South Korea, in the upper panel, I set  $\gamma = 0.167$ ,  $\gamma^* = 0.0025$ ,  $\kappa = 6.8$ ,  $\sigma_a = 3.98$ , and  $\rho_{a,a^*} = 0.73$ ; in the calibration for South Korea, in the upper panel, I set  $\gamma = 0.167$ ,  $\gamma^* = 0.0025$ ,  $\kappa = 6.8$ ,  $\sigma_a = 3.98$ , and  $\rho_{a,a^*} = 0.73$ ; in the calibration for South Korea, in the

	Belgium ( $\gamma = 0.253$ )				
	$\phi^e=0$	$\phi^e = 0.37$	$\phi^e = 0.555$	$\phi^e = 0.74$	
	Model	Model	Model	Model	
$corr(\Delta e_t, \Delta q_t)$	0.99	0.99	1.00	1.00	
$\sigma(\Delta e_t)/\sigma(\Delta g dp_t)$	1.0	1.2	1.3	1.8	
$\sigma(\Delta e_t)/\sigma(\Delta c_t)$	2.2	2.5	2.8	3.6	
$\sigma(\Delta n x_t) / \sigma(\Delta q_t)$	0.60	0.50	0.42	0.29	
Price and Wage Stickiness	YES	YES	YES	YES	
$corr(\Delta e_t, \Delta q_t)$	0.83	0.93	0.96	0.99	
$\sigma(\Delta e_t)/\sigma(\Delta g dp_t)$	1.8	2.0	2.0	2.1	
$\sigma(\Delta e_t)/\sigma(\Delta c_t)$	2.1	2.4	2.6	3.2	
$\sigma(\Delta n x_t) / \sigma(\Delta q_t)$	1.33	0.76	0.50	0.27	
Price and Wage Stickiness	NO	NO	NO	NO	

Table 6: Sensitivity Analysis with Exporter-Importer Firms for Belgium

Notes: Each cell in the second, third, fourth, and fifth columns of the table is the median value of moments across 10,000 simulations of 120 quarters; I choose  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to respectively match the targeted moments  $std(\Delta z_t)/std(\Delta y_t) = 2.5$ ,  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , and  $corr(\Delta y_t, \Delta y_t^*) = 0.35$ . In calibration with  $\phi^e = 0$ , in the upper panel, I set  $\kappa = 5$ ,  $\sigma_a = 5.24$ , and  $\rho_{a,a^*} = 0.41$ ; in calibration with  $\phi^e = 0$ , in the lower panel, I set  $\kappa = 22$ ,  $\sigma_a = 4$ , and  $\rho_{a,a^*} = 0.16$ ; in calibration with  $\phi^e = 0.37$ , in the upper panel, I set  $\kappa = 3.8$ ,  $\sigma_a = 4.49$ , and  $\rho_{a,a^*} = 0.66$ ; in calibration with  $\phi^e = 0.37$ , in the upper panel, I set  $\kappa = 19$ ,  $\sigma_a = 3.74$ , and  $\rho_{a,a^*} = 0.23$ ; in calibration with  $\phi^e = 0.555$ , in the upper panel, I set  $\kappa = 3.8$ ,  $\sigma_a = 4.22$ , and  $\rho_{a,a^*} = 0.71$ ; in calibration with  $\phi^e = 0.555$ , in the upper panel, I set  $\kappa = 16$ ,  $\sigma_a = 3.79$ , and  $\rho_{a,a^*} = 0.30$ ; in calibration with  $\phi^e = 0.74$ , in the upper panel, I set  $\kappa = 12$ ,  $\sigma_a = 3.84$ , and  $\rho_{a,a^*} = 0.38$ . The last row of each panel indicates whether the model is calibrated taking price and wage stickiness à la Calvo (1983) into account.

Floating Regime $(\omega_e = 0)$	US Moments	No Exporter-Importer Firms $(\phi^e=0)$	Exporter-Importer Firms ( $\phi^e=0.74$ )
		United S	States
		$\gamma = 0$	.07
$\sigma(\Delta e_t)/\sigma(\Delta g dp_t)$	5.2	3.4	5.8
$\sigma(\Delta q_t) / \sigma(\Delta exports_t)$	5.4	0.94	3.42
$\sigma(\Delta q_t) / \sigma(\Delta imports_t)$	5.4	0.94	3.43
$\sigma(\Delta n x_t) / \sigma(\Delta q_t)$	0.10	0.17	0.08
Price and Wage Stickiness		YES	YES

#### Table 7: Net-Exports Decomposition without and with Exporter-Importer Firms

Notes: The first and the fourth US empirical moments in the second column are respectively from Tables 1 and 3 in Itskhoki and Mukhin (2021); the second and the third US empirical moments in the second column are from Section 2.  $exports_t = y_{Ht}^*$  without exporter-importer firms and  $exports_t = y_{Ht}^* + e_{Ht}$  with exporter-importer firms.  $imports_t = y_{Ft}$  without exporter-importer firms and  $imports_t = y_{Ft} + e_{Ft}^*$  with exporter-importer firms.  $imports_t = y_{Ft}$  without exporter-importer firms and  $imports_t = y_{Ft} + e_{Ft}^*$  with exporter-importer firms. Each cell in the third and fourth columns of the table is the median value of moments across 10,000 simulations of 120 quarters; I choose  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to respectively match the targeted moments  $std(\Delta z_t)/std(\Delta y_t) = 2.5$ ,  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , and  $corr(\Delta y_t, \Delta y_t^*) = 0.35$ . In the calibration in the third column of the table, I set  $\kappa = 6.8$ ,  $\sigma_a = 2.5$ , and  $\rho_{a,a^*} = 0.37$  to match the targeted moments in the model of Itskhoki and Mukhin (2021) with  $\gamma = 0.07$ ; in the calibration in the fourth column of the table, I set  $\kappa = 5.4$ ,  $\sigma_a = 1.52$ , and  $\rho_{a,a^*} = 0.6$  to match the targeted moments in my model with exporter-importer firms with  $\gamma = 0.07$ . The last row of the table indicates whether the model is calibrated when taking price and wage stickiness à la Calvo (1983) into account.

Pegged Regime	$\omega_e = 0.23$	Belgian Moments
$corr(\Delta e_t, \Delta q_t)$	0.99	0.61
$\sigma(\Delta e_t)/\sigma(\Delta y_t)$	1.38	1.10
$\sigma(\Delta e_t)/\sigma(\Delta c_t)$	2.08	1.39
$\sigma(\Delta n x_t) / \sigma(\Delta q_t)$	0.27	0.88
Floating Regime	$\omega_e = 0$	Belgian Moments
Floating Regime $corr(\Delta e_t, \Delta q_t)$	$\omega_e = 0$ 0.99	Belgian Moments 0.95
$corr(\Delta e_t, \Delta q_t)$	0.99	0.95

Table 8: Quantitative Results for Belgium acrossExchange-Rate Regimes

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Notes: The Belgian moments in the third column are from Section 2. Each cell in the second column is the median value of moments across 10,000 simulations of 120 quarters; I choose  $\kappa = 9$ ,  $\sigma_a = 2.9$ , and  $\rho_{a,a^*} = 0.45$  to respectively match the targeted moments  $std(\Delta z_t)/std(\Delta y_t) = 2.5$ ,  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , and  $corr(\Delta y_t, \Delta y_t^*) = 0.35$  under the floating regime; I set  $\omega_e = 0.23$ , as in Itskhoki and Mukhin (2025), under the pegged regime.

#### 3.4 Cross-Country Empirical Evidence on Exporter-Importer Firms

Given the importance that my model assigns to the presence of importer-exporter firms, this section documents cross-country empirical evidence in support of the theoretical mechanism. Although the presence of exporterimporter firms has been documented in countries which have different trade-to-GDP ratios, documenting this phenomenon both across countries and over time is challenging since firm-product-level databases on imports and exports are limited to recent years and few countries. To overcome this lack of data availability, I propose the following macro-to-micro approach. At the macro level, starting from the gross trade flows of all the thirty countries taken into consideration in the empirical facts of Section 2, I show a systematic positive correlation between exports and imports over time from 1957 to 2019. At the microeconomic level, in reverse chronological order, I list several works on the presence of exporter-importer firms, taking advantage of the more recent literature which uses firm-product-level databases on imports and exports from European and non-European G20 countries.

#### 3.4.1 Evidence from the Gross Trade Flows

Table 13 in Appendix A.3.4 reports, for each of the thirty countries in Section 2, the correlation between its export and import shares, which I use to obtain the trade-weighted exchange rates in Section 2.1.<sup>26</sup> Although displaying heterogeneity across countries, the second and third columns of Table 10 in Appendix A.3.4 indicate a systematic positive correlation between bilateral exports and imports for each country over time. This result represents a necessary, albeit not sufficient, condition for the presence of exporter-importer firms.

#### 3.4.2 Evidence from Firm-Product-Level Databases

Wicht and Yeşin (2025), using an unpublished database including information about 11,600 firms from 2016 to 2022, which represent the largest exporter and importer firms in the Swiss customs data, finds that 91% of exporter firms are also importer firms. Specifically, along the import-size distribution, 96% of firms above the median also export, 97.3% of firms above the 75% percentile also export, and 99.7% of firms above the 90% percentile also export.

Blaum (2024, pp. 2445-2446) evaluates the mechanism of exporter-importer firms by relying on firm-level data after two large devaluations, the Mexican devaluation in 1995 and the Indonesian devaluation in 1998.<sup>27</sup> First, for both Mexico and Indonesia, exporter firms account for more than the totality of the aggregate import share growth for almost all the time horizons following the devaluation, implying that the contribution of firms which sell domestically tends to reduce the aggregate import share.

<sup>&</sup>lt;sup>26</sup>For any given country, I use as share the values of its exports and imports from the Direction of Trade Statistics of the International Monetary Fund, averaged over the 1957-2019 period, to and from Australia, Austria, Belgium, Canada, Denmark, Finland, France, Germany, Greece, Ireland, Italy, Japan, Luxembourg, the Netherlands, Norway, Portugal, Spain, Sweden, Switzerland, the United Kingdom, and the United States.

<sup>&</sup>lt;sup>27</sup>For the empirical analysis employing firm-product-level data, the author takes into consideration the years from 1995 to 1999 for Mexico and the years from 1998 to 2000 for Indonesia, see Table IV in Blaum (2024, p. 2445).

Second, for the exporter firms that (before the devaluation) import intensively, the expansion (after the devaluation) tends to be fully accounted for by their additional exporting activity. Taken together, these two findings suggest that the exporter-importer firms play a crucial role in changing the patterns of reallocation and aggregate substitution after these two large devaluations.

Barbiero (2022, pp. 10-11), using a database containing information on customs activities and balance sheets for French firms from 2000 to 2017, finds that, at the firm level, exporter firms simultaneously engage in both import and export activities. In France, over that time period, the top one-hundred exporter firms account for a share of total exports of 47.30% and the top one-thousand exporter firms account for a share of total exports of 73.99%. The author shows that, after accounting for within-firm operational hedging of the exporter firms, the overall macro pricing exposure related to the French extra-EU trade is reduced. However, as they decrease in size, exporter firms tend to avoid foreign-priced transactions, but the few foreign-priced exports, for smaller exporter firms, still match with foreign-priced imports.

Albornoz and Garcia-Lembergman (2020, pp. 6-7), uses customs data on 14,636 manufacturing firms, comprising the universe of exports and imports transactions in Argentina from 2002 to 2009. In such a dataset, the median exporter-importer firm exports 180,000 US dollars and imports 113,000 US dollars.

Amiti, Itskhoki, and Konings (2014, pp. 1958-1959) uses Belgian firm-product-level data on imports and exports between 2000 and 2008. First, the authors find evidence that 78% of exporter firms in Belgium also import goods and, more crucially, that the exporter firms who intensively import goods account for 83% of all Belgian exports. Second, they show that the ratio between imported inputs and exports is 74% for the import-intensive exporter firms. In other words, the import-intensive exporter firms account for a disproportionately large share of exports and keep their prices unchanged despite exchange-rate volatility, thanks to the imported inputs in the marginal-cost channel.

Bernard et al. (2007, pp. 124-125), using 1997 for U.S. firms that appear in both the U.S. Census of Manufactures and the Linked-Longitudinal Firm Trade Transaction Database, shows that, looking across industries, there is a strong correlation (0.87) between industries with high shares of importing firms and those with high shares of exporters. The authors also find that, for 1997, 41% of exporting firms also import while 79% of importers also export in the United States. All these works are summarized in Table 9, which reports the references, the analyzed countries and time period of each study.<sup>28</sup>

<sup>&</sup>lt;sup>28</sup>Other works–Alfaro, Calani, and Varela (2021), Kasahara and Lapham (2013)–also document the presence of exporter-importer firms in Chile over the 2005-2018 period and the 1990-1996 period, respectively. I do not include such works in Table 7 since Chile is not a European country, neither a non-European G20 country.

Paper	Country	Time Period
Wicht and Yeşin (2025)	Switzerland	2016-2022
Blaum (2024, pp. 2444-46)	Indonesia, Mexico	1998-2000 (Indonesia), 1995-1999 (Mexico)
Barbiero (2022, pp. 10-11)	France	2000-2017
Albornoz and Garcia-Lembergman (2020, pp. 6-7)	Argentina	2002-2009
Amiti, Itskhoki, and Konings (2014, pp. 1958-59)	Belgium	2000-2008
Bernard et al. (2007, pp. 124-125)	United States	1997

#### Table 9: Empirical Literature on the Exporter-Importer Firms

# 4 Conclusion

How should researchers think about exchange-rate regimes? In this paper, consistently with the previous literature on the Mussa puzzle and exchange rate disconnect, I show that such regimes affect the volatilities of nominal and real exchange rates but not the volatilities of other real macro variables, even for economies that have larger exports and imports, compared to total output, than the United States. I also provide a set of assumptions under which modeling this muted reaction is possible, and I show how this result crucially relies on exporters also being firms that intensively import. In the future, I plan to investigate two further questions.

First, is the import intensity of the exporter-importer firms a structural parameter of the economy—as I assume in my model—or is it endogenous to the exchange-rate regime? In other words, does  $\phi^e$  adjust at the time of an exchange-rate regime break that modifies the volatility of the nominal exchange rate? The question has to be systematically investigated at the micro level by asking: how do firms adjust their production function immediately before and after an exchange-rate regime break that changes the volatility of the nominal exchange rate? The model developed here could be easily extended to account for this additional feature of firm optimization.

Second, I emphasize that the exogenous shock in the exchange-rate regime appears in the theoretical model, and its calibration, as a different value of parameter  $\omega_e$ . This is not necessarily true in the case of a regime break that endogenously arises in response to conditions that are exogenous to the two economies.

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# Appendix for

"The Macro Neutrality of Exchange-Rate Regimes

in the presence of Exporter-Importer Firms"

## A.2 - Empirical Facts and Exchange-Rate Regimes

Country	Exchange Rates	Real Macro Variables
Australia <sup>a</sup>	1/1957-12/2019	1/1960-12/2019
Austria	1/1957-12/2019	1/1960-12/2019
Dalaina	1/1057 10/2010	1/10/0 19/2010
Belgium	1/1957-12/2019	1/1960-12/2019
Brazil	12/1979-12/2019	1/1996-12/2019
Canada	1/1957-12/2019	1/1961-12/2019
Culludu	1,1,0,1,10,1,201,	1, 1, 01 12, 201,
Czech Republic	3/1993-12/2019	1/1994-12/2019
Denmark <sup>b</sup>	1/1957-12/2019	1/1960-12/2019
Estonia	2/1993-12/2019	1/1995-12/2019
Finland <sup>c</sup>	1/1957-12/2019	1/1960-12/2019
France <sup>d</sup>	1/1957-12/2019	1/1960-12/2019

 Table 10: Available Time Periods for the Macro Variables

*Notes:* <sup>a</sup>The monthly consumer price index is missing, I construct it by linear interpolation using the quarterly consumer price index. <sup>b</sup>The monthly consumer price index from January 1957 to December 1966 is missing, I construct it by linear interpolation using the quarterly consumer price index. <sup>c</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from January 1963 to December 2019 in the series that significantly depart from the rest, I run it only over the period from January 1959 to December 2019 in the monthly time series.

Country	Exchange Rates	Real Macro Variables
Germany	1/1957-12/2019	1/1960-12/2019
Greece	1/1957-12/2019	1/1960-12/2019
Ireland <sup>e</sup>	1/1957-12/2019	1/1960-12/2019
Italy <sup>f</sup>	1/1957-12/2019	1/1960-12/2019
Japan	1/1957-12/2019	1/1960-12/2019
Latvia	6/1993-12/2019	1/1995-12/2019
Lithuania	9/1993-12/2019	1/1995-12/2019
Luxembourg	1/1957-12/2019	1/1960-12/2019
Netherlands <sup>g</sup>	1/1957-12/2019	1/1960-12/2019
Norway	1/1957-12/2019	1/1960-12/2019

*Notes:* <sup>e</sup>The monthly consumer price index from January 1957 to December 1996 is missing, I construct it by linear interpolation using the quarterly consumer price index. <sup>f</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from January 1959 to December 2019 in the monthly time series. <sup>g</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from January 1959 to December 2019 in the series that significantly depart from the rest, I run it only over the period from January 1960 to December 2019 in the monthly time series.

Country	Exchange Rates	Real Macro Variables
Poland <sup>h</sup>	1/1988-12/2019	1/1995-12/2019
Portugal <sup>i</sup>	1/1957-12/2019	1/1960-12/2019
Slovak Republic	3/1993-12/2019	1/1993-12/2019
Slovenia <sup>j</sup>	3/1992-12/2019	1/1995-12/2019
South Africa		
	12/1963-12/2019	1/1960-12/2019
Spain <sup>k</sup>	1/1957-12/2019	1/1960-12/2019
Sweden	1/1957-12/2019	1/1960-12/2019
Switzerland	1/1957-12/2019	1/1960-12/2019
United Kingdom	1/1957-12/2019	1/1957-12/2019
United States	1/1957-12/2019	1/1957-12/2019

*Notes*: <sup>h</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from January 1990 to December 2019 in the monthly time series. <sup>i</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from January 1959 to December 2019 in the monthly time series. <sup>j</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from January 1959 to December 2019 in the monthly time series. <sup>j</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from March 1992 to December 2006 in the monthly time series. <sup>k</sup>Given that the Lavielle (1999) and Lavielle and Moulines (2000) test is particularly sensitive to observations in the series that significantly depart from the rest, I run it only over the period from January 1960 to December 2019 in the monthly and quarterly time series; the bilateral nominal exchange rate in March 1964 is missing, I construct it by linear interpolation.

#### A.2.1 - A Characterization of Exchange-Rate Regimes

I apply the test developed by Lavielle (1999) and Lavielle and Moulines (2000) to empirically identify structural breaks in the volatility of the nominal- and real-exchange-rate series. It is an extension of the Bai and Perron (1998) test for weakly and strongly dependent processes and is used to simultaneously detect structural breaks in the volatility of a time series when the number of structural breaks is unknown. I preliminarily remove the outliers from the  $\Delta e_t$  ( $\Delta q_t$ ) series to properly apply the heteroskedasticity-break test, defining outliers as elements more than three local standard deviations away from the local mean within a forty-nine-month window that is centered about the current element and contains forty-eight neighboring months.<sup>29</sup>

The Lavielle (1999) and Lavielle and Moulines (2000) test. Denote  $X_t = \Delta e_t$  (or  $X_t = \Delta q_t$ ), t = 1, 2, 3, ..., T. Assume that the unknown number of segments K in the time series is upper bounded by a known finite  $\overline{K}$ . Lavielle (1999) and Lavielle and Moulines (2000) propose to estimate the configuration of structural breaks  $\tau$  and the number of segments K by minimizing the penalized-contrast function as follows:

$$(\hat{\tau}_T, \hat{K}_T) = \arg\min_{1 \le K \le \bar{K}} \inf_{\tau \in \mathcal{T}_K} \left\{ \frac{1}{T} \sum_{k=1}^K \left( \frac{||\mathbf{X}_k||^2}{\sigma_k^2} + T_k \ln \sigma_k^2 \right) + \beta_T K \right\}.$$

Here,  $\mathbf{X}_k$  is the vector of observations that belong to segment k in the configuration  $\tau = (\tau_k, 1 \le k \le K - 1), T_k$ is the length of  $\mathbf{X}_k, \sigma_k^2$  is the variance of  $X_t$  in segment k, and  $\beta_T K$  is the penalization term. In my analysis, I set  $\overline{K} = 6$ , which implies a maximum of five structural breaks, and I choose  $\beta_T$  according to Lavielle (1999, p. 81).

<sup>&</sup>lt;sup>29</sup>The heteroskedasticity-break test does not always identify the structural breaks in the volatility of the nominal- and real-exchange-rate series in the same month since it is very sensitive to observations that significantly depart from the rest.

Country	Nominal Exchange Rate	Real Exchange Rate	Exchange-Rate Regime
Australia	January 1957 - December 1970	January 1957 - November 1972	Pegged Regime
	January 1971 - December 2019	December 1972 - December 2019	Floating Regime
Austria	January 1957 - November 1970	January 1957 - December 1972	Pegged Regime
	December 1970 - October 1979	January 1973 - March 1979	Floating Regime
	November 1979 - July 1992	April 1979 - July 1992	Pegged Regime
	August 1992 - August 1998	August 1992 - March 1997	Floating Regime
	September 1998 - December 2019	April 1997 - December 2019	Pegged Regime
Brazil	December 1979 - August 1994	December 1979 - November 1994	Floating Regime
	September 1994 - July 1998	December 1994 - November 1996	Pegged Regime
	August 1998 - December 2019	December 1996 - December 2019	Floating Regime
Canada	January 1957 - April 1970	January 1957 - December 1972	Pegged Regime
	May 1970 - December 2019	January 1973 - December 2019	Floating Regime
Czech Republic	March 1993 - December 2012	March 1993 - October 2012	Floating Regime
	January 2013 - December 2019	November 2012 - December 2019	Pegged Regime
Denmark	January 1957 - December 1972	January 1957 - November 1972	Pegged Regime
	January 1973 - December 1978	December 1972 - December 1977	Floating Regime
	January 1979 - July 1992	January 1978 - July 1992	Pegged Regime
	August 1992 - September 1997	August 1992 - February 1997	Floating Regime
	October 1997 - December 2019	March 1997 - December 2019	Pegged Regime

### Table 11: Exchange-Rate Regimes

Country	Nominal Exchange Rate	Real Exchange Rate	Exchange-Rate Regime
Estonia	February 1993 - March 1998	February 1993 - April 1997	Floating Regime
	April 1998 - December 2019	May 1997 - December 2019	Pegged Regime
Finland	January 1963 - June 1971	January 1963 - April 1971	Pegged Regime
	July 1971 - March 1983	May 1971 - May 1983	Floating Regime
	April 1983 - September 1991	June 1983 - October 1991	Pegged Regime
	October 1991 - July 1997	November 1991 - April 1997	Floating Regime
	August 1997 - December 2019	May 1997 - December 2019	Pegged Regime
France	January 1959 - July 1969	January 1959 - July 1971	Pegged Regime
	August 1969 - March 1978	August 1971 - March 1983	Floating Regime
	April 1978 - July 1992	April 1983 - July 1992	Pegged Regime
	August 1992 - August 1998	August 1992 - July 1997	Floating Regime
	September 1998 - December 2019	August 1997 - December 2019	Pegged Regime
Germany	January 1957 - November 1970	January 1957 - December 1972	Pegged Regime
	December 1970 - September 1978	January 1973 - February 1981	Floating Regime
	October 1978 - July 1992	March 1981 - July 1992	Pegged Regime
	August 1992 - March 1998	August 1992 - March 1997	Floating Regime
	April 1998 - December 2019	April 1997 - December 2019	Pegged Regime

Country	Nominal Exchange Rate	Real Exchange Rate	Exchange-Rate Regime
Greece	January 1957 - July 1970	January 1957 - December 1970	Pegged Regime
	August 1970 - October 2000	January 1971 - July 1995	Floating Regime
	November 2000 - December 2019	August 1995 - December 2019	Pegged Regime
Ireland	January 1957 - November 1970	January 1957 - August 1972	Pegged Regime
	December 1970 - September 1981	September 1972 - February 1982	Floating Regime
	October 1981 - July 1992	March 1982 - July 1992	Pegged Regime
	August 1992 - October 1998	August 1992 - March 1998	Floating Regime
	November 1998 - December 2019	April 1998 - December 2019	Pegged Regime
Italy	January 1959 - December 1972	January 1959 - December 1972	Pegged Regime
	January 1973 - April 1981	January 1973 - July 1983	Floating Regime
	May 1981 - May 1992	August 1983 - May 1992	Pegged Regime
	June 1992 - December 1998	June 1992 - May 1996	Floating Regime
	January 1999 - December 2019	June 1996 - December 2019	Pegged Regime
Japan	January 1957 - July 1971	January 1957 - January 1973	Pegged Regime
	August 1971 - December 2019	February 1973 - December 2019	Floating Regime
Latvia	June 1993 - December 2004	June 1993 - March 2004	Floating Regime
	January 2005 - December 2019	April 2004 - December 2019	Pegged Regime
Lithuania	September 1993 - January 2002 February 2002 - December 2019	September 1993 - February 2002 March 2002 - December 2019	Floating Regime Pegged Regime

Country	Nominal Exchange Rate	Real Exchange Rate	Exchange-Rate Regime
Luxembourg	January 1957 - June 1971	January 1957 - December 1972	Pegged Regime
	July 1971 - September 1978	January 1973 - January 1980	Floating Regime
	October 1978 - July 1992	February 1980 - July 1992	Pegged Regime
	August 1992 - March 1998	August 1992 - April 1996	Floating Regime
	April 1998 - December 2019	May 1996 - December 2019	Pegged Regime
Netherlands	January 1960 - March 1971	January 1960 - December 1972	Pegged Regime
	April 1971 - December 1978	January 1973 - May 1978	Floating Regime
	January 1979 - July 1992	June 1978 - July 1992	Pegged Regime
	August 1992 - March 1998	August 1992 - May 1997	Floating Regime
	April 1998 - December 2019	June 1997 - December 2019	Pegged Regime
Norway	January 1957 - June 1971	January 1957 - December 1972	Pegged Regime
	July 1971 - December 2019	January 1973 - December 2019	Floating Regime
Poland	January 1990 - July 2012	January 1990 - April 2012	Floating Regime
	August 2012 - December 2019	May 2012 - December 2019	Pegged Regime
Portugal	January 1959 - June 1971	January 1959 - July 1971	Pegged Regime
	July 1971 - September 1986	August 1971 - October 1975	Floating Regime
	October 1986 - May 1991	November 1975 - May 1978	Pegged Regime
	June 1991 - March 1998	June 1978 - June 1997	Floating Regime
	April 1998 - December 2019	July 1997 - December 2019	Pegged Regime

Country	Nominal Exchange Rate	Real Exchange Rate	Exchange-Rate Regime
Slovak Republic	March 1993 - December 2008	March 1993 - December 2008	Floating Regime
	January 2009 - December 2019	January 2009 - December 2019	Pegged Regime
Slovenia	March 1992 - July 1997	March 1992 - May 1998	Floating Regime
	August 1997 - December 2019	June 1998 - December 2019	Pegged Regime
South Africa	December 1963 - November 1970	December 1963 - February 1970	Pegged Regime
	December 1970 - December 2019	March 1970 - December 2019	Floating Regime
Spain	January 1960 - September 1968	January 1960 - January 1973	Pegged Regime
	October 1968 - April 1998	February 1973 - May 1996	Floating Regime
	May 1998 - December 2019	June 1996 - December 2019	Pegged Regime
Sweden	January 1957 - February 1973	January 1957 - February 1973	Pegged Regime
	March 1973 - December 2019	March 1973 - December 2019	Floating Regime
Switzerland	January 1957 - August 1970	January 1957 - November 1972	Pegged Regime
	September 1970 - December 2019	December 1972 - December 2019	Floating Regime
United Kingdom	January 1957 - November 1970	January 1957 - August 1972	Pegged Regime
	December 1970 - December 2019	September 1972 - December 2019	Floating Regime
United States	January 1957 - June 1971	January 1957 - July 1971	Pegged Regime
	July 1971 - December 2019	August 1971 - December 2019	Floating Regime

## A.3 - Theoretical Framework

#### A.3.1 - Model

#### A.3.1.1 - Home Country

**Households.** The solution to the consumption-savings problem of the representative household can be obtained by formulating a Lagrangian. Combining the first-order conditions of the Lagrangian and the accumulation rule for the capital stock results in the Euler equation, the labor supply equation, and the asset pricing equation:

$$C_t^{-\sigma} = \beta R_t \mathbb{E}_t \left[ \frac{C_{t+1}^{-\sigma}}{P_{t+1}} \right] P_t, \tag{8}$$

$$C_t^{\sigma} L_t^{1/\varphi} = \frac{W_t}{P_t}$$
, and (9)

$$\left(1+\kappa\frac{\Delta K_{t+1}}{K_t}\right)C_t^{-\sigma} = \beta \mathbb{E}_t \left\{ \left(C_{t+1}^{-\sigma}\right) \left[\frac{R_{t+1}^K}{P_{t+1}} - \delta + \left(1+\kappa\frac{\Delta K_{t+2}}{K_{t+1}}\right) + \frac{\kappa}{2}\frac{\left(\kappa\frac{\Delta K_{t+2}}{K_{t+1}}\right)^2}{2\kappa}\right] \right\}.$$
 (10)

**Domestic firms.** The solution to the cost minimization of the representative domestic firm results in the following demands for labor, capital, and intermediate inputs:

$$W_t L_{Dt} = (1 - \phi)(1 - \vartheta)MC_{Dt}Y_{Ht},\tag{11}$$

$$R_t^K K_{Dt} = (1 - \phi) \vartheta M C_{Dt} Y_{Ht}, \text{ and}$$
(12)

$$P_t X_{Dt} = \phi M C_{Dt} Y_{Ht}.$$
(13)

**Exporter-importer firms.** The solution to the cost minimization of the representative exporter-importer firm results in the following demands for labor, capital, intermediate inputs, and directly imported inputs:

$$W_t L_{Et} = (1 - \phi^e)(1 - \phi)(1 - \vartheta)MC_{Et}Y_{Ht}^*,$$
(14)

$$R_t^K K_{Et} = (1 - \phi^e)(1 - \phi)\vartheta M C_{Et} Y_{Ht}^*,$$
(15)

$$P_t X_{Et} = (1 - \phi^e) \phi M C_{Et} Y_{Ht}^*, \text{ and}$$
(16)

$$\mathcal{E}_t P_{Ft}^* E_{Ft}^* = \phi^e M C_{Et} Y_{Ht}^*. \tag{17}$$

#### A.3.1.5 - Equilibrium Definition and Model Solution

Equilibrium in the Nonlinear Model. Given the exogenous shocks  $\{a_t, a_t^*\}$ , the policy specifications for the sequence of gross nominal interest rates  $\{R_t, R_t^*\}$ , and the targeted nominal exchange rate  $\{\bar{\mathcal{E}}\}$ , an equilibrium in the nonlinear model is a collection of stochastic processes for  $\{Y_t, Y_t^*, Y_{Ht}, Y_{Ft}, Y_{Ht}^*, Y_{Ft}^*, C_t, C_t^*, L_t, L_t^*, K_t, K_t^*, X_t, X_t^*, P_t, P_t^*, \mathcal{P}_t, \mathcal{P}_t^*, P_{Ht}, P_{Ft}, P_{Ht}^*, P_{Ft}^*, W_t, W_t^*, R_t^K, R_t^{K^*}, Q_t, Q_t^*, B_t, B_t^*, \mathcal{E}_t\}$  that solves the price indexes (1) and (2); the optimal pricing equations (3) and (4); the Euler equation (8); the labor supply equation (9); the asset pricing equation (10); the domestic firm demands for labor (11), capital (12), and intermediate inputs (13); the exporter-importer firm demands for labor (14), capital (15), intermediate inputs (16), and directly imported inputs (17); their respective counterparts in the foreign country; the market clearing conditions for labor, capital, and goods in the foreign country; and the market clearing conditions in the international financial markets.

#### A.3.2 - Exporter-Importer Firms Resolving Exchange Rate Disconnect

**Proof.**<sup>30</sup> The labor supply (9) and labor demand (11, 14) equations are:

$$\sigma c_t + \varphi^{-1} l_t = w_t - p_t$$
, and

$$w_t + l_t = (1 - \tau)(mc_t + y_{Ht}) + \tau(mc_{Et} + y_{Ht}^*).$$

Here,  $\tau \equiv (1 - \phi^e)\gamma$ . Combining the two to solve for  $l_t$ , and using the expressions for the marginal costs and the optimal pricing equations, results in:

$$\varphi \sigma c_t + \left[ (1-\tau) y_{Ht} + \tau y_{Ht}^* \right] = (1+\varphi) a_t - \left[ \frac{\varphi + \phi}{1-\phi} \iota + \tau \phi^e (1+2\iota - \alpha \iota) \right] q_t.$$

Here,  $\iota \equiv \frac{\tilde{\gamma}(1-\delta)(1-\alpha)(1-\tilde{\gamma})+[\tilde{\gamma}(1-\delta)]^2}{[(1-\alpha)(1-\tilde{\gamma})]^2-[\tilde{\gamma}(1-\delta)]^2}$  and  $\delta \equiv \frac{\alpha(1-\tilde{\gamma})+(1-\alpha)\phi^e}{1-\tilde{\gamma}[1-(1-\alpha)\phi^e]}$ . Subtracting the symmetric equation for the foreign country yields to the following equation that characterizes the supply side:

$$\varphi\sigma(c_t - c_t^*) + \left[(1 - \tau)(y_{Ht} - y_{Ft}^*) + \tau(y_{Ht}^* - y_{Ft})\right] = (1 + \varphi)(a_t - a_t^*) - 2\left[\frac{\varphi + \phi}{1 - \phi}\iota + \tau\phi^e(1 + 2\iota - \alpha\iota)\right]q_t.$$
 (18)

Combining the demands in each good market, and using the demands for intermediate inputs and directly imported intermediate inputs, yields to the following equation that characterizes the demand side:

$$[(1-\tau)(y_{Ht} - y_{Ft}^*) + \tau(y_{Ht}^* - y_{Ft})] = \frac{(1-\phi)(1-2\tau)}{1+\phi(2\tau-1)}(c_t - c_t^*) + \frac{2\zeta}{1+\phi(2\tau-1)}q_t.$$
 (19)

 $<sup>^{30}</sup>$ I prove the result in the model with no capital in the same fashion of Itskhoki and Mukhin (2021, 2025).

Here,

$$\begin{aligned} \zeta \equiv &(1-\tau)\frac{1-\gamma}{(1-\gamma)+\phi^e\gamma} \left\{ \theta(1-\alpha)\iota + \phi \left[\phi^e\tau(1+2\iota-\alpha\iota)-\iota\right] \right\} + \\ &(1-\tau)\frac{\phi^e\gamma}{(1-\gamma)+\phi^e\gamma} \left\{ \left[1-\phi^e(1-\phi\tau)\right](1+2\iota-\alpha\iota) - \theta(1-\delta)(1+\iota) - \phi\iota \right\} + \\ &\tau \left\{\phi \left[\phi^e\tau(1+2\iota-\alpha\iota)-\iota\right] - \theta(1-\delta)(1+\iota) \right\}. \end{aligned}$$

Combining equations (18) and (19) to solve for  $c_t-c_t^\ast$  results in:

$$c_t - c_t^* = \frac{(1+\varphi)\left[1+\phi(2\tau-1)\right]}{\varphi\sigma\left[1+\phi(2\tau-1)\right]+(1-\phi)(1-2\tau)} (a_t - a_t^*) + \\ -2\frac{1+\phi(2\tau-1)}{\varphi\sigma\left[1+\phi(2\tau-1)\right]+(1-\phi)(1-2\tau)} \left[\frac{\varphi+\phi}{1-\phi}\iota + \tau\phi^e(1+2\iota-\alpha\iota) + \frac{\zeta}{1+\phi(2\tau-1)}\right] q_t.$$

Then,  $c_t - c_t^* = \frac{(1+\varphi)}{1+\varphi\sigma}(a_t - a_t^*)$  if  $\phi^e \to 1$ .

Non-Calibrated Parameter	Variable	Value	Source
Household discount factor	β	0.99	
Relative risk aversion	$\sigma$	2	
Inverse Frisch elasticity	$\varphi$	1	
Intermediate inputs share	$\phi$	0.5	
Capital share	θ	0.3	
Import intensity of exporter-importer firms	$\phi^e$	0.74	Amiti, Itskhoki, and Konings (2014)
International-Trade openness for the United States	$\gamma$	0.07	
International-Trade openness for Belgium	$\gamma$	0.253	Belgian Imports-to-GDP ratio = 0.506
International-Trade openness for New Zealand	$\gamma$	0.114	
International-Trade openness for the United Kingdom	$\gamma$	0.122	
International-Trade openness for Sweden	$\gamma$	0.165	
International-Trade openness for South Korea	$\gamma$	0.167	
Elasticity of substitution	$\theta$	1.5	
Strategic complementarity	$\alpha$	0.4	
Interest rate smoothing	ho	0.95	
Inflation rate targeting	$\omega_{\pi}$	2.15	
Nominal exchange rate targeting, under pegged regimes	$\omega_e$	0.23	Itskhoki and Mukhin (2025)
Persistence of the shocks	$ ho_a, ho_{a^*}, ho_\psi$	0.97	
Standard deviation of financial shocks	$\chi_1 \sigma_\psi$	1	
Net Foreign Asset Coefficient in equation (5)	$\chi_2$	0.001	
Calvo probability for prices	$\lambda_p$	0.75	
Calvo probability for wages	$\lambda_w$	0.85	
Calibrated Parameter	Variable		Targeted Moment
Capital adjustment cost Standard deviation of productivity shocks	$\kappa$ $\sigma_a,\sigma_{a^*}$	$\rightarrow$ $\rightarrow$	$std(\Delta z_t)/std(\Delta y_t) = 2.5$ $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$
Correlation of productivity shocks	$ ho_{a,a^*}$	$\rightarrow$	$corr(\Delta y_t, \Delta y_t^*) = 0.35$

#### Table 12: Model Parameters

Notes: The non-calibrated parameters are taken from Itskhoki and Mukhin (2021) if not differently specified; for details on the values of the calibrated parameters see Tables 4, 5, and 6 in Section 3.3: I choose  $\kappa$ ,  $\sigma_a$ , and  $\rho_{a,a^*}$  to respectively match the targeted moments  $std(\Delta z_t)/std(\Delta y_t) = 2.5$ ,  $corr(\Delta q_t, \Delta c_t - \Delta c_t^*) = -0.4$ , and  $corr(\Delta y_t, \Delta y_t^*) = 0.35$  under the floating regime.

## A.3.4 - Cross-Country Empirical Evidence on Exporter-Importer Firms

### A.3.4.1 - Evidence from the Gross Trade Flows

Country Full Period Minimum / Maximum Australia 0.62 / 0.91 0.78 Austria 0.99 0.91 / 1.00 Belgium 0.91 0.87 / 1.00 Brazil 0.81 / 0.99 0.96 Canada 1.00 0.99 / 1.00 Czech Republic 1.00 0.99 / 1.00 Denmark 0.87 / 0.99 0.96 Estonia 0.80 / 0.98 0.93 Finland 0.93 0.81 / 0.97 France 0.98 0.80 / 0.99 Germany 0.73 / 0.97 0.95 Greece 0.72 / 0.97 0.97 Ireland 0.99 0.64 / 1.00 Italy 0.98 0.83 / 0.99 Japan 0.97 0.97 / 1.00

Table 13: Cross-Country Correlation of Gross Trade Flows

Country	Full Period	Minimum / Maximum
Latvia	0.81	0.62 / 0.87
Lithuania	0.92	0.58 / 0.98
Luxembourg	0.83	0.71 / 0.98
Netherlands	0.96	0.89 / 0.98
Norway	0.78	0.40 / 0.95
Poland	0.99	0.81 / 0.99
Portugal	0.93	0.72 / 0.98
Slovak Republic	1.00	0.95 / 0.99
Slovenia	0.97	0.93 / 0.98
South Africa	0.87	0.71 / 0.91
Spain	0.94	0.67 / 0.98
Sweden	0.91	0.79 / 0.97
Switzerland	0.97	0.77 / 1.00
United Kingdom	0.96	0.62 / 0.97
United States	0.97	0.87 / 0.99

*Notes:* The second column shows the correlation between the export and import weights, averaged over the 1957-2019 period, for each of the thirty countries in Section 2. The third column shows the minimum and the maximum values of the correlation, between the export and imports weights of each of the thirty countries in Section 2, when the latter is calculated for each year from 1957 to 2019.